

# 1 **Distributed neural dynamics underlie the shift from** 2 **movement preparation to execution**

3 **Ziwei Yin** <sup>1,2\*</sup>, **Jian K. Liu** <sup>1,2</sup>, **Katja Kornysheva** <sup>1,3\*</sup>

4 <sup>1</sup>Center for Human Brain Health, University of Birmingham, Birmingham, UK

5 <sup>2</sup>School of Computer Science, University of Birmingham, Birmingham, UK

6 <sup>3</sup>School of Psychology, University of Birmingham, Birmingham, UK

7 \*Correspondence: [zxy370@student.bham.ac.uk](mailto:zxy370@student.bham.ac.uk), [k.kornysheva@bham.ac.uk](mailto:k.kornysheva@bham.ac.uk)

8 **Dissociating the neural mechanisms of movement preparation from those of execution across**  
9 **the brain is fundamental to understanding motor control. Invasive recordings in primary motor**  
10 **cortex (M1) indicate that shared neural populations support both phases by unfolding within**  
11 **orthogonal subspaces or "manifolds", yet whether and how these dynamics evolve across**  
12 **the broader set of brain regions involved in memory-guided skilled action remains poorly**  
13 **understood. Here, we used magnetoencephalography (MEG) data obtained during a memory-**  
14 **guided delayed finger-sequence task to track fast population dynamics across M1, premotor**  
15 **cortices, and the hippocampus. Linear discriminant analysis decoding of sequence-specific**  
16 **preparatory and execution patterns revealed a transition from preparation to execution pat-**  
17 **terns across all regions prior to movement onset. Importantly, the onset of execution exhib-**  
18 **ited region-specific timing, with M1 shifting last, ~100 ms before the first button press, con-**  
19 **sistent with the established cortical motor hierarchy. Low-dimensional trajectories showed**  
20 **that preparatory and execution states occupied distinct manifolds, yet were not fully orthog-**  
21 **onal, suggesting partial overlap in tuning. MEG dynamics were dominated by peri-movement**  
22 **phase activity in the primary motor and premotor regions. Nevertheless, above-chance se-**  
23 **quence decoding was recoverable from all motor and premotor regions during execution and**  
24 **in M1 during preparation. The state shift and the decoding accuracy were driven by distributed**  
25 **modulations across multiple frequency bands, indicating that full-band population dynamics**  
26 **carry richer information than band-limited features alone. These results demonstrate that**  
27 **non-invasive MEG can resolve continuous, hierarchical neural state transitions in the human**  
28 **brain in the context of memory-guided movement control. They offer mechanistic insight into**  
29 **distributed motor-related brain dynamics and support developing brain-computer-interfaces**  
30 **that incorporate signals from multiple brain regions beyond the primary motor cortex.**

31 **Keywords: motor control, preparation, manifolds, neural dynamics, MEG, source reconstruction**

## 32 1. Introduction

33 Coordinating skilled actions requires the nervous system to prepare upcoming movements while  
34 preventing their premature release [1]. In non-human primates, invasive recordings in the primary  
35 motor (M1) and adjacent areas have shown that preparation and execution are implemented through  
36 distinct population-level neural states that unfold within separate low-dimensional subspaces of the  
37 same motor population [2–4]. Preparatory activity evolves in an "output-null" space, enabling the  
38 retrieval of motor plans without immediate motor output, while execution occupies an "output-potent"  
39 space defined by characteristic rotational dynamics [2, 3, 5, 6]. These findings support a dynamical-  
40 systems view in which actions emerge from evolving population trajectories, i.e., dynamic response  
41 patterns rather than static tuning of individual neurones to upcoming movement features activated  
42 below or above a threshold [7].

43 In humans, neuroimaging can reveal large scale activity pattern transitions from preparation to  
44 execution across the brain. Here, fMRI results suggest that the control of sequence features un-  
45 dergoes a state shift from high-level feature separation during planning to their integration during  
46 execution across a network of motor-related cortical and subcortical areas [8, 9]. However, the tem-  
47 poral dynamics and geometry of this transition remain unknown. MEG/EEG provide non-invasive  
48 access to brain dynamics, including well-established oscillatory markers of movement preparation,  
49 such as beta and alpha ( $\mu$ )-band desynchronisation before and during movement linked to cortical  
50 excitability, followed by their post-movement rebound linked to inhibition [10–13] and theta-band  
51 activity associated with cognitive control and memory-dependent planning [14, 15]. However, these  
52 oscillatory dynamics alone do not reveal whether preparation and execution patterns occupy distinct  
53 neural manifolds, nor how the transition between them unfolds across distributed brain regions.

54 Skilled actions typically require the integration of hierarchical information spanning movements  
55 sequence structure, chunk organisation and individual movements [15, 16]. Prior work shows that  
56 these levels are not represented uniformly across the motor system: M1 primarily encodes upcoming  
57 single movements [17–19], whereas lateral and medial premotor regions contain sequence-selective  
58 activity [8, 20, 21]. Further, there is growing evidence of the hippocampus supporting retrieval and  
59 control of sequential order [9, 22, 23], with hippocampal–cortical replay predicting short-term perfor-  
60 mance gains [24]. Together, this distributed architecture suggests that sequence preparation from  
61 memory recruits both motor and cognitive brain areas.

62 Invasive studies have largely focused on M1 and PMd, leaving it unclear how these and other  
63 motor sequence-relevant regions coordinate the transition from preparation to execution. Whether the  
64 preparatory–execution manifolds observed in M1 extend across cortical and hippocampal networks,  
65 and how their dynamics unfold in time, remains unknown.

66 Here, we examined source-resolved MEG obtained during a memory-guided finger-sequence  
67 task to probe the preparatory–execution state transition non-invasively and access its organisation  
68 across motor, premotor and hippocampal regions. We further asked whether oscillatory MEG dynam-  
69 ics track the transition and support the decoding of upcoming sequence identity. Our results reveal  
70 a global shift across distinct manifolds toward execution-related patterns prior to movement onset,  
71 with evidence of hierarchical timing across premotor and primary motor regions, and sequence-  
72 specific information detectable in primary motor areas even before movement execution. These  
73 results demonstrate that non-invasive MEG can resolve continuous, hierarchical state transitions and  
74 reveal distributed population dynamics underlying sequential action in the human brain.

## 2. Results

### 2.1. Oscillatory markers of motor excitation, inhibition and serial recall converge in M1

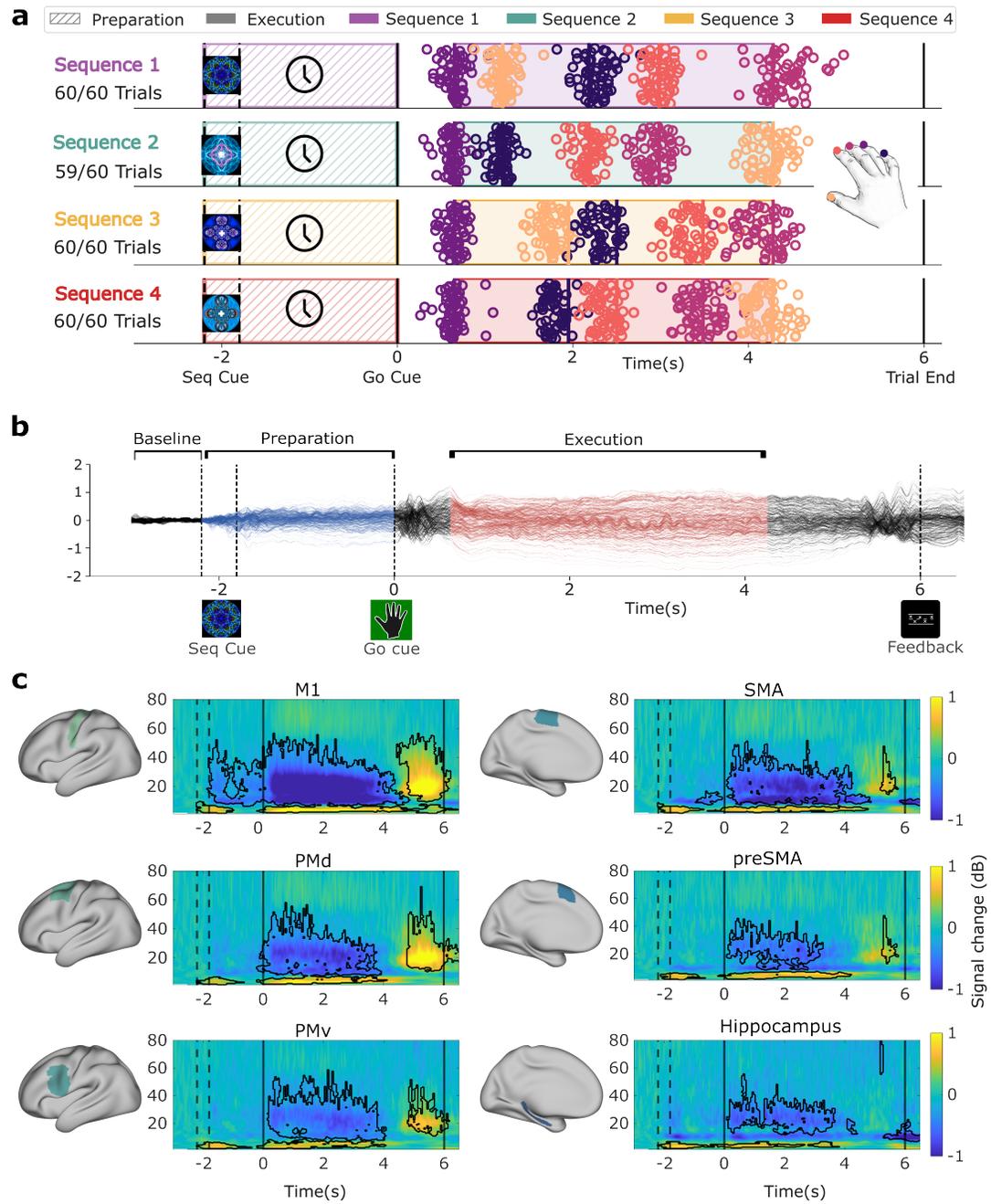
To dissociate the preparatory and executive patterns that support memory-guided sequential movements across motor and hippocampal circuits, we analysed the MEG dataset from Kornysheva et al. [25]. In a delayed finger sequence task, participants learned to retrieve a five-element finger sequence and its associated target timing from memory cued by an abstract visual stimulus (Sequence Cue), and then to execute the sequence on a response keyboard following a Go Cue (Fig. 1a). We applied linearly constrained minimum variance (LCMV) beamforming to localise neural activity from regions of interest reported in our recent fMRI studies involving a similar paradigm [8, 9] - the contralateral primary motor cortex (M1), dorsal premotor cortex (PMd), supplementary motor area (SMA), ventral premotor cortex (PMv), pre-supplementary motor area (pre-SMA), and the hippocampus (Fig. 1c).

As expected, we observed neurophysiological markers of movement-related neural excitation and inhibition [13] - beta and alpha ( $\mu$ ) band event-related desynchronisation (ERD) during sequence preparation and execution, and a post-movement beta rebound (PMBR, Fig. 1c). Here, M1 was the only region with significant ERD during the preparation phase. ERD in M1 started on average 1.6 seconds prior to the Go Cue and lasted until the end of execution -1.6 – 3.8 s, 9 – 46 Hz,  $p < .001$ . This effect followed smaller ERD clusters in premotor areas: PMd (0.2 – 3.1 s, 9 – 47.5 Hz,  $p < .001$ ), PMv (0.2 – 3.85 s, 9 – 35 Hz,  $p < .001$ ), SMA (0.2 – 4.15 s, 8.5 – 44.5 Hz,  $p < .001$ ), and pre-SMA (0.15 – 1.05 s, 18.5 – 37.5 Hz,  $p = .001$ ; 1.15 – 3.1 s, 9.5 – 37 Hz,  $p < .001$ ).

PMBR showed the most pronounced modulation in contralateral M1 (4.9 – 5.85 s, 14 – 46.5 Hz,  $p = .006$ ) and PMd (4.85 – 6.5 s, 12.5 – 48.5 Hz,  $p = .003$ ), followed by PMv (4.9 – 5.85 s, 18 – 39.5 Hz,  $p = .012$ ), SMA (5.3 – 5.5 s, 19 – 44 Hz,  $p = .019$ ), and pre-SMA (5.3 – 5.6 s, 15.5 – 43.5 Hz,  $p = .014$ ). Several beta desynchronisation clusters distributed across the execution period were also found in the hippocampus (0.15 – 1.15 s, 17.5 – 51 Hz,  $p < .001$ ; 1.35 – 3.65 s, 13 – 39.5 Hz,  $p < .001$ ; 4.1 – 4.2 s, 17 – 21.5 Hz,  $p = .035$ , 5.35 – 6.7 s, 7.5 – 19.5 Hz,  $p = .002$ ), but no PMBR. Instead, the hippocampus showed a high-gamma cluster after movement termination (5.2 – 5.25 s, 59.5 – 80 Hz,  $p = .01$ ).

Increases in theta- and delta-band power were observed across all regions during both preparation and execution, in line with their role in memory and serial recall and their expected distribution across both hippocampal and cortical sources [26, 27]. Clusters were found in M1 (-1.9 – -1.3 s, 2 – 5 Hz,  $p = .043$ ; 0.1 – 5.7 s, 2.5 – 5 Hz,  $p = .015$ ); PMd (-1.85 – -1.1 s, 2 – 4.5 Hz,  $p = .035$ ; 0.15 – 3.45 s, 2.5 – 5.5 Hz,  $p = .013$ ); PMv (-2 – -0.95 s, 2 – 5.5 Hz,  $p = .02$ ; 0.05 – 3.45 s, 2.5 – 5.5 Hz,  $p = .01$ ); SMA (-1.95 – -1.1 s, 2.5 – 6 Hz,  $p = .018$ ; 0.1 – 4.15 s, 2.5 – 5.5 Hz,  $p = .006$ ); pre-SMA (-1.9 – -1.0 s, 1.5 – 5.5 Hz,  $p = .011$ ; -0.1 – 4.05 s, 2 – 6.5 Hz,  $p < .001$ ); and the the hippocampus (-2 – -0.55 s, 2 – 6.5 Hz,  $p = .004$ ; -0.05 – 2.55 s, 3 – 6 Hz,  $p = .002$ ; 3.05 – 3.5 s, 3 – 6.5 Hz,  $p = .029$ ).

These time-frequency results confirm the predicted oscillatory markers in motor, premotor and hippocampal regions during a memory-guided motor sequence tasks. Further, they indicate that contralateral M1, the principal cortical output area, is pre-activated during sequence preparation and shows all task-related band modulations observed in upstream areas.



## Figure 1: Delayed finger sequence task and time frequency representations

**(a)** Task design and representative behavioural data from a single participant. Participants memorised four five-finger tapping sequences over two days before the MEG sessions. The sequences formed a factorial combination of two temporal interval patterns and two finger orderings. During the recording session, each sequence was performed 60 times, with incorrect trials excluded from analysis. The data is aligned to the Go Cue; two black dash vertical line mark the variable delay period (1.8, 2.0, or 2.2 s) between the Sequence Cue and the Go Cue. Raster dots represent individual finger presses on each trial, colour-coded by finger identity. The coloured vertical bars indicate the planned timing of each finger press in the memorised sequence. Only trials classified as correct were shown and included in subsequent analyses. **(b)** Overview of task structure and MEG channel activity averaged across trials and participants. The blue colour indicates the preparation phase spanning the Sequence Cue and the Go Cue; the red colour indicates the execution phase between the first finger press and the last press. **(c)** Time-frequency representations (TFRs) showing source-localised oscillatory dynamics from six regions of interest: M1, PMd, SMA, pre-SMA, PMv and hippocampus. Each panel is paired with the anatomical mask used for source reconstruction. Individual TFRs were baseline-corrected using decibel (dB) normalisation relative to each participant's own baseline period, then group-averaged and baseline demeaned. Black contours indicate significant time–frequency clusters relative to baseline.

## 2.2. Timing of the transition from preparation to execution patterns

To uncover the timing of the neural transition between sequence preparation and execution states, we trained and tested a linear discriminant analysis (LDA) classifier with eight classes on trial-by-trial MEG patterns, including each of the four sequences during preparation and execution, respectively, from each of the six regions. For LDA training, we defined the preparatory phase as the period between the Sequence cue and the Go Cue. The execution phase was defined as the period between the first and the last press (Fig. 2a). If sequence tuning generalised across phases, classifier accuracy of sequence execution-specific patterns would have matched those during preparation, and vice versa. Alternatively, the two representations would be specific to their LDA training phase only.

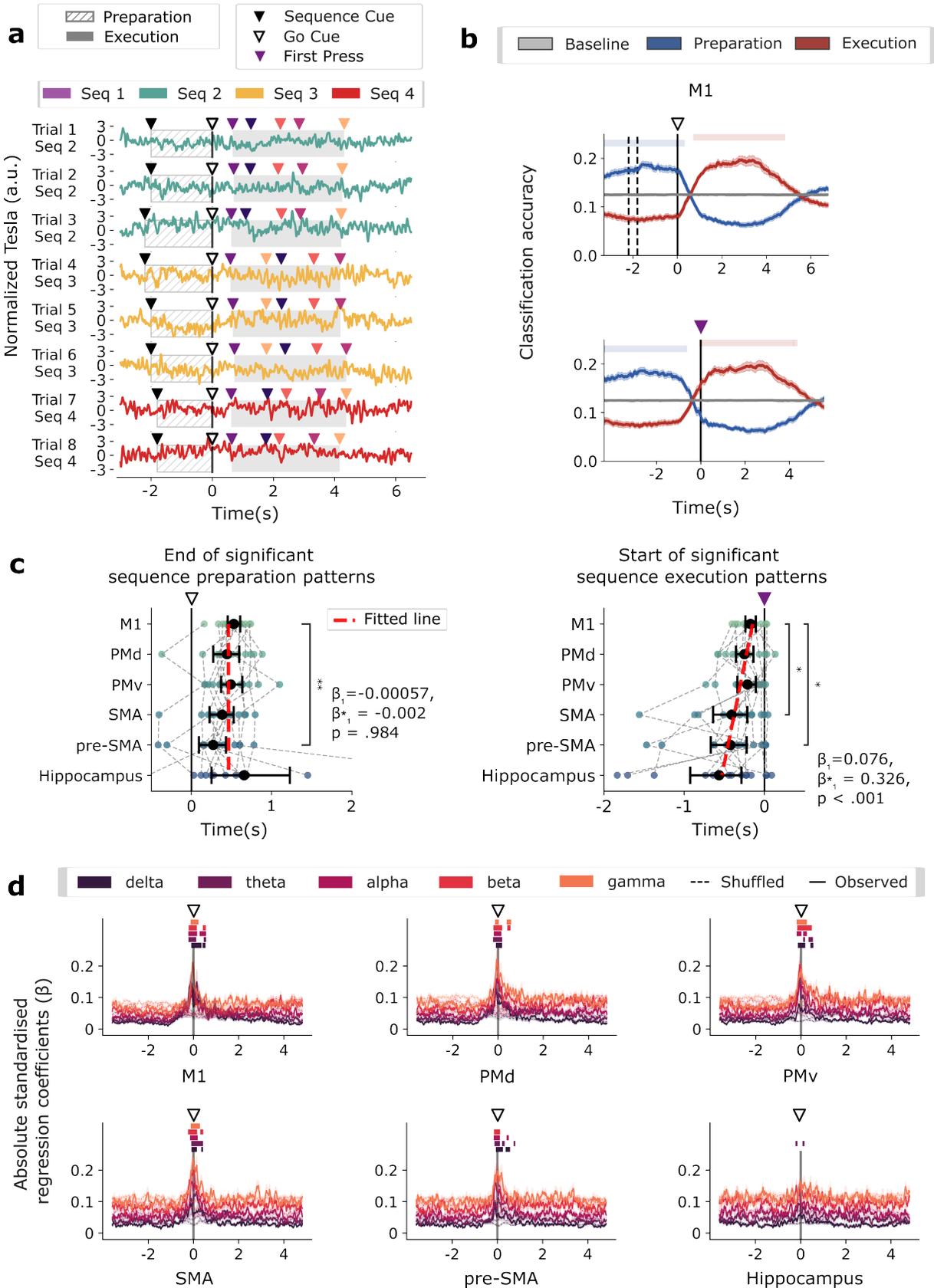
The resulting sequence probability time courses showed distinct and temporally non-overlapping sequence patterns (Fig.2 b-c): execution related sequence classification accuracy remained below chance during the preparatory period, including shortly after the Go Cue, and rose significantly above chance only shortly before execution. Preparatory tuning showed the opposite pattern, with a brief gap in between phases where neither phase reached significance. This stark result confirmed that the preparation and execution phases are associated with distinct neural sequence tuning patterns that do not generalise across phases.

To resolve the timing of the offset of the preparatory sequence patterns and the onset of the execution patterns above chance, the classifier probabilities were aligned to two behavioural anchors: the Go Cue and the first movement (button press). Significance testing against temporally permuted predictions showed that neural transitions consistently occurred after the Go Cue and before movement initiation (Fig.2 b-c). The offset of sequence preparation patterns was quantified for each region: M1:  $0.52 \pm 0.19$  s; PMd:  $0.41 \pm 0.31$  s; PMv:  $0.44 \pm 0.23$  s; SMA:  $0.41 \pm 0.33$  s; pre-SMA:  $0.32 \pm 0.33$  s; hippocampus:  $0.22 \pm 1.05$  s (Fig.2d, upper panel). Pairwise Wilcoxon rank-sum tests confirmed a significant difference between M1 and pre-SMA,  $p = .001$ . Similarly, the onset of the sequence execution patterns differed across regions: M1:  $-0.14 \pm 0.13$  s; PMd:  $-0.23 \pm 0.23$  s; PMv:  $-0.16 \pm 0.17$  s; SMA:  $-0.39 \pm 0.43$  s; pre-SMA:  $-0.62 \pm 0.64$  s; hippocampus:  $-0.62 \pm 0.62$  s (Fig.2d, lower panel). Pairwise Wilcoxon rank-sum tests confirmed a significant difference between M1 and pre-SMA ( $p = .010$ ), and M1 versus SMA: ( $p = .048$ ).

To investigate whether the timing of the neural patterns transitions followed the motor hierar-

145 chy, we fitted linear mixed-effects models. The hierarchical order was defined by the proximity of  
146 regions to the periphery, i.e. in line with the reported anatomical density of direct cortico-spinal  
147 projections to the lower cervical segments of the spinal cord (C7–T1) and cortico-cortical connec-  
148 tivity to M1, from furthest to closest: Hippocampus, pre-SMA, SMA, PMv, PMd and M1. Whilst  
149 the offset of preparation patterns showed no evidence of a hierarchical shift [28] ( $\beta_0 = 0.465, \beta_1 =$   
150  $-0.00057, \beta_1^* = -0.002, p = .984$ ), the onset of execution revealed a significant positive slope, with  
151 transitions occurring progressively later along the motor hierarchy, with M1 transitioning last to exe-  
152 cution patterns ( $\beta_0 = -0.607, \beta_1 = 0.077, \beta_1^* = 0.326, p < .001$ ).

153 When the execution prediction curve was correlated with spectral power in different canonical  
154 frequency bands, most significant clusters were clustered around the phase transition (Fig.2e). Sig-  
155 nificant M1 clusters observed in delta ( $-0.11 - 0.34$  s,  $p < .001$ ;  $0.40 - 0.54$  s,  $p = .025$ ), theta ( $-0.23$   
156  $- 0.13$  s,  $p = .003$ ;  $0.45 - 0.57$  s,  $p = .020$ ), alpha ( $-0.24 - 0.17$  s,  $p = .002$ ;  $0.27 - 0.56$  s,  $p = 0.002$ ),  
157 beta ( $-0.22 - 0.15$  s,  $p = .005$ ;  $0.41 - 0.55$  s,  $p = 0.033$ ), gamma ( $-0.14 - 0.23$  s,  $p = .004$ ). PMd  
158 observed significant delta ( $-0.11 - 0.18$  s,  $p = 0.005$ ), theta ( $-0.23 - 0.19$  s,  $p < .001$ ), alpha ( $-0.20$   
159  $- 0.15$  s,  $p = .002$ ), beta ( $-0.22 - 0.19$  s,  $p = .002$ ;  $0.40 - 0.55$  s,  $p = .023$ ), gamma ( $-0.15 - 0.04$  s,  
160  $p = .015$ ;  $0.38 - 0.58$  s,  $p = .021$ ) clusters. PMv also observed significant clusters in all frequency  
161 bands, delta ( $-0.15 - 0.20$  s,  $p = .001$ ;  $0.42 - 0.55$  s,  $p = .039$ ), theta ( $0.09 - 0.19$  s,  $p = .020$ ;  $0.33$   
162  $- 0.54$  s,  $p = .003$ ), alpha ( $-0.20 - 0.03$  s,  $p = .005$ ;  $0.09 - 0.27$  s,  $p = .022$ ), beta ( $-0.18 - 0.48$  s,  
163  $p = .001$ ), gamma ( $-0.20 - 0.27$  s,  $p = .001$ ). SMA observed delta ( $-0.10 - 0.16$  s,  $p = .002$ ;  $0.34$   
164  $- 0.43$  s,  $p = .032$ ), theta ( $-0.11 - 0.43$  s,  $p = .002$ ), alpha ( $-0.16 - 0.20$  s,  $p = .001$ ), beta ( $-0.25$   
165  $- 0.17$  s,  $p = .002$ ), gamma ( $-0.13 - 0.29$  s,  $p = .002$ ). Pre-SMA observed delta ( $-0.08 - 0.25$  s,  
166  $p = .001$ ;  $0.34 - 0.57$  s,  $p = .003$ ), theta ( $-0.14 - 0.12$  s,  $p = .002$ ;  $0.21 - 0.33$  s,  $p = 0.035$ ;  $0.72 -$   
167  $0.80$  s,  $p = .040$ ), alpha ( $-0.17 - 0.12$  s,  $p < .001$ ;  $0.40 - 0.51$  s,  $p = 0.030$ ), gamma ( $-0.16 - 0.13$  s,  
168  $p = .004$ ). Hippocampus only showed significant correlation in theta band ( $-0.24 - -0.14$  s,  $p = .017$ ;  
169  $0.08 - 0.18$  s,  $p = .017$ ).



**Figure 2: LDA quantifies temporal transitions between motor preparation and execution. (a)** Schematic of the eight-class Linear Discriminant Analysis (LDA) training. The LDA discriminates between combinations of sequence identity and phase (e.g., Seq1 x Prep, Seq2 x Exec) and is trained on 200 Hz raw source dynamics taken from individual trials based on the variable Go Cue delay and finger presses. The plot shows example data from one channel over 12 trials. Sampling windows were aligned to trial-specific behavioural markers, with an equal number of samples drawn from each phase. To account for class imbalance, 40 trials were sampled per sequence, and results were averaged over 1,000 bootstrap repetitions. **(b)** LDA classification accuracy across participants ( $n = 14$ ) for M1, aligned to the Go Cue (top) or the first button press (bottom). Curves reflect the probability assigned to the correct sequence–phase class (e.g., Seq1-Prep / Seq1-Exec for sequence-1 trials). Traces indicate participant averages, with shaded regions denoting standard error. Semi-transparent shading at the top of each plot marks significant intervals relative to the shuffled baseline (cluster forming alpha  $< .01$ , final threshold  $< .05$ ). Preparatory and execution predictions exhibit temporally non-overlapping patterns. **(c)** The timing of offset of significant preparation patterns aligned to go cue (Top) and the timing of onset of significant execution patterns aligned to first press (Bottom) across motor areas and the hippocampus. Connecting lines represent data from individual participants ( $n = 14$ ). Statistical comparisons were performed using Wilcoxon rank-sum tests with BH–FDR correction across 15 comparisons. Red dashed lines show the fitted linear mixed-effects models computed from subject-averaged transition timings. Corresponding model outputs are added in the text next to panels. **(d)** Rectified standardised regression coefficients relating the execution-probability time course to canonical frequency-band activity. Colours denote frequency bands. Shading at the top of each plot marks significant intervals relative to the permuted-correlation baseline (circular-shift null, averaged over 1,000 permutations). Both the execution-probability time course and the TFR-derived band-power signals were z-scored across the whole trial prior to correlation. Correlations were computed using a sliding window (200 ms window, 10 ms step).

### 170 **2.3. Principal component analysis reveal distinct preparation and execution mani-** 171 **olds**

172 Next, we applied principal component analysis (PCA) to embed high-dimensional source MEG dy-  
173 namics into three-dimensional manifolds. This approach reveals the geometric structure underlying  
174 movement-related dynamics across multiple brain regions, enabling a more direct comparison with  
175 invasive animal recordings [2, 5]. The first three principal components captured the majority of the  
176 variance across all regions (Fig.3; M1:  $90.5 \pm 3.3\%$ ; PMd:  $94.9 \pm 1.7\%$ ; PMv:  $93.3 \pm 2.2\%$ ; SMA:  
177  $97.5 \pm 1.1\%$ ; pre-SMA:  $97.7 \pm 0.7\%$ ; hippocampus:  $99.2 \pm 0.3\%$ ).

178 When projected into this low-dimensional space, trajectories from the preparation and execu-  
179 tion phases occupied distinct manifolds, showing differential distributions between phases along the  
180 principal component axes (Fig.3a). This phase separation was confirmed by statistically significant  
181 Kolmogorov–Smirnov (KS) distances between the preparation and execution distributions along each  
182 PC axis, evaluated against a permutation-based null distribution and present in all regions of inter-  
183 est (Fig.3b; Wilcoxon signed-rank tests, false discovery rate controlled using Benjamini-Hochberg  
184 (FDR-BH) across  $6 \text{ areas} \times 3 \text{ PCs}$ ; all  $p < .001$ ).

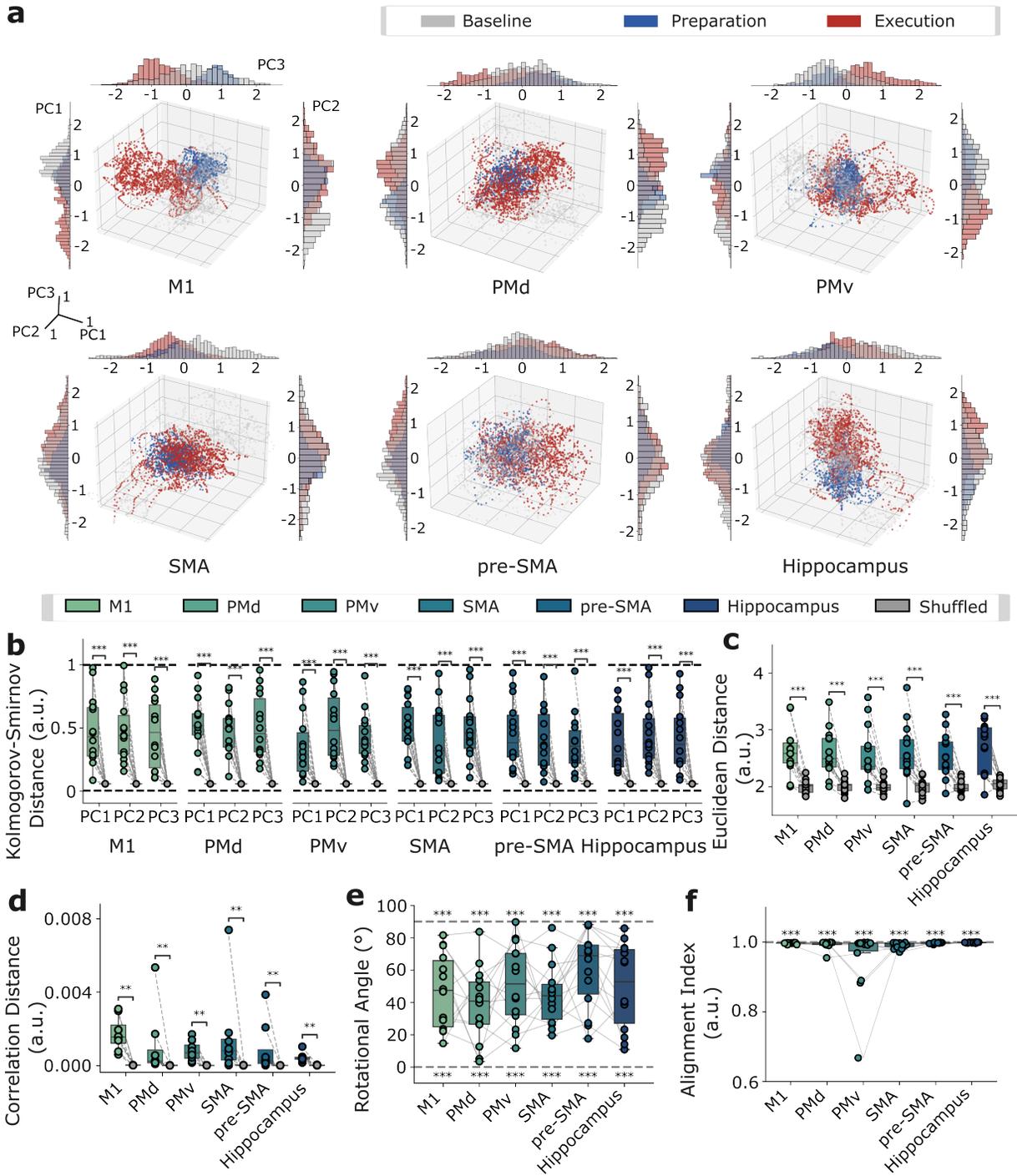
185 Furthermore, the Euclidean distance between the phase clusters in the low-dimensional space  
186 was significantly greater than chance in all regions (Fig.3c; Wilcoxon signed-rank tests; Bonferroni  
187 corrected across 6 regions; M1:  $2.31 \pm 0.43$ ,  $p < .001$ ; PMd:  $2.30 \pm 0.42$ ,  $p < .001$ ; PMv:  $2.27 \pm 0.45$ ,  
188  $p = .002$ ; SMA:  $2.30 \pm 0.48$ ,  $p = .001$ ; pre-SMA:  $2.27 \pm 0.39$ ,  $p = .001$ ; hippocampus:  $2.36 \pm 0.46$ ,  
189  $p = .001$ ). The largest separations were observed in M1 and the hippocampus, with slightly smaller  
190 distances in the remaining motor regions. There were no significant differences in distances between  
191 areas (Friedman test:  $\chi^2(5) = 2.12$ ,  $p = .832$ ).

192 PCA was computed using covariance matrices averaged across the full trial. To test whether the

193 preparatory and execution periods nevertheless exhibit distinct covariance patterns, we computed  
194 covariance matrices in a sliding-window fashion and quantified the similarity between preparatory and  
195 execution matrices. The correlation metric is unchanging with respect to scale; therefore, the distance  
196 between phases indicates that execution is not simply a weaker or scaled version of preparation. In  
197 all regions, the correlation between preparatory and execution covariance matrices was significantly  
198 lower than expected by chance (Fig.3d; Wilcoxon signed-rank tests against permutation; Bonferroni  
199 corrected across 6 regions;  $p = .004$  for all regions; M1:  $0.0017 \pm 0.0009$ ; PMd:  $0.0011 \pm 0.0017$ ; PMv:  
200  $0.0008 \pm 0.0005$ ; SMA:  $0.0016 \pm 0.0023$ ; pre-SMA:  $0.0009 \pm 0.0013$ ; hippocampus:  $0.0004 \pm 0.0002$ ).  
201 The Friedman test indicated a significant effect of region,  $\chi^2(5) = 11.14$ ,  $p = .049$ , but no pairwise  
202 Wilcoxon signed-rank comparisons survived FDR-BH across 15 area pairs.

203 Previous research highlighted the geometric orthogonality between the preparatory and execution  
204 dynamics [3]. To examine this in our data, we fitted a Gaussian mixture model (GMM) to each  
205 state within the three-dimensional PCA space and compared the angles between their respective  
206 hyperplanes (Fig. 3e). The resulting angles were neither parallel ( $0^\circ$ ) nor orthogonal ( $90^\circ$ ) to each  
207 other (M1:  $46.7 \pm 23.1^\circ$ ; PMd:  $38.4 \pm 22.8^\circ$ ; PMv:  $51.2 \pm 24.9^\circ$ ; SMA:  $45.1 \pm 19.2^\circ$ ; pre-SMA:  $60.6 \pm$   
208  $24.0^\circ$ ; hippocampus:  $50.0 \pm 26.3^\circ$ ; Wilcoxon signed-rank tests, Bonferroni-corrected across 6 regions;  
209  $p < .001$  for all comparisons).

210 Following the established subspace analysis [4], we projected the subspace defined by execution-  
211 only dynamics onto the subspace derived from preparation-only dynamics. The resulting alignment  
212 index revealed that the preparatory and execution dynamics occupy highly similar low-dimensional  
213 manifolds, as reflected by the high alignment index (Fig. 3e; M1:  $0.997 \pm 0.0019$ ; PMd:  $0.994 \pm 0.011$ ;  
214 PMv:  $0.956 \pm 0.088$ ; SMA:  $0.955 \pm 0.0085$ ; pre-SMA:  $0.998 \pm 0.0018$ ; Hippocampus:  $0.999 \pm 0.0010$ ).  
215 However, when tested against the perfect alignment (index = 1), all areas showed alignment indices  
216 significantly below 1 (Wilcoxon signed-rank tests, Bonferroni-corrected across 6 regions; all  $p < .001$ ).  
217 Moreover, the group passed the Friedman test ( $\chi^2(5) = 16.735$ ;  $p = .005$ ) and hippocampus exhibited  
218 higher alignment than motor areas (PMv vs. hippocampus:  $p = .005$ ; SMA vs. hippocampus:  $p =$   
219  $.009$ ; Wilcoxon rank-sum tests, BH-FDR corrected across 15 comparisons).



**Figure 3: Preparation and execution occupy distinct subspaces in shared low-dimension manifold. (a)** Source-localised MEG data projected onto the first three principal components for an example participant. All axes were z-scored. Trajectories show sequence-averaged dynamics, colour-coded by phase (preparation, execution). Marginal histograms indicate the distribution of data points along each principal component axis for each phase. **(b)** Kolmogorov–Smirnov (KS) distances between preparatory and execution dynamics along individual principal components. The KS distance (range: 0–1) quantifies the maximum difference between the empirical distributions of two samples. Each dot represents one participant ( $N = 14$ ). The mean distance for each participant is generated by bootstrap in which 500 data points were drawn, and the KS distance was bootstrapped across 1,000 iterations. A permutation test was performed by randomly reassigning samples between phases to generate a null distribution. **(c)** Euclidean distance between preparatory and execution trajectories in the 3D PCA space. For each participant, the mean distance from execution points to the preparatory centroid was compared to a null distribution obtained by randomly permuting phase labels (500 samples per group, 1,000 iterations). **(d)** Correlation distance between phase-average covariance matrices indicate significant phase difference (Wilcoxon signed-rank tests, Bonferroni-corrected across 6 regions;  $p < .01$  for all comparisons). **(e)** Angle between the directions of maximum variance of the preparatory and execution Gaussian mixture models (GMMs). This angle reflects the difference in orientation between the two dominant axes of variation. The resulting angles were neither parallel ( $0^\circ$ ) nor orthogonal ( $90^\circ$ ) to each other (Wilcoxon signed-rank tests, Bonferroni-corrected across 6 regions;  $p < .001$  for all comparisons). **(f)** Alignment index quantifying the similarity between neural manifolds formed by preparatory and execution dynamics. Values approaching 1 indicate stronger alignment, suggesting that both phases occupy similar subspaces. Wilcoxon signed-rank test against full alignment (1) is  $p < .001$  for all areas (Bonferroni correction over 6 areas).

## 220 2.4. MEG covariance pattern separation is driven by phase, not sequence identity

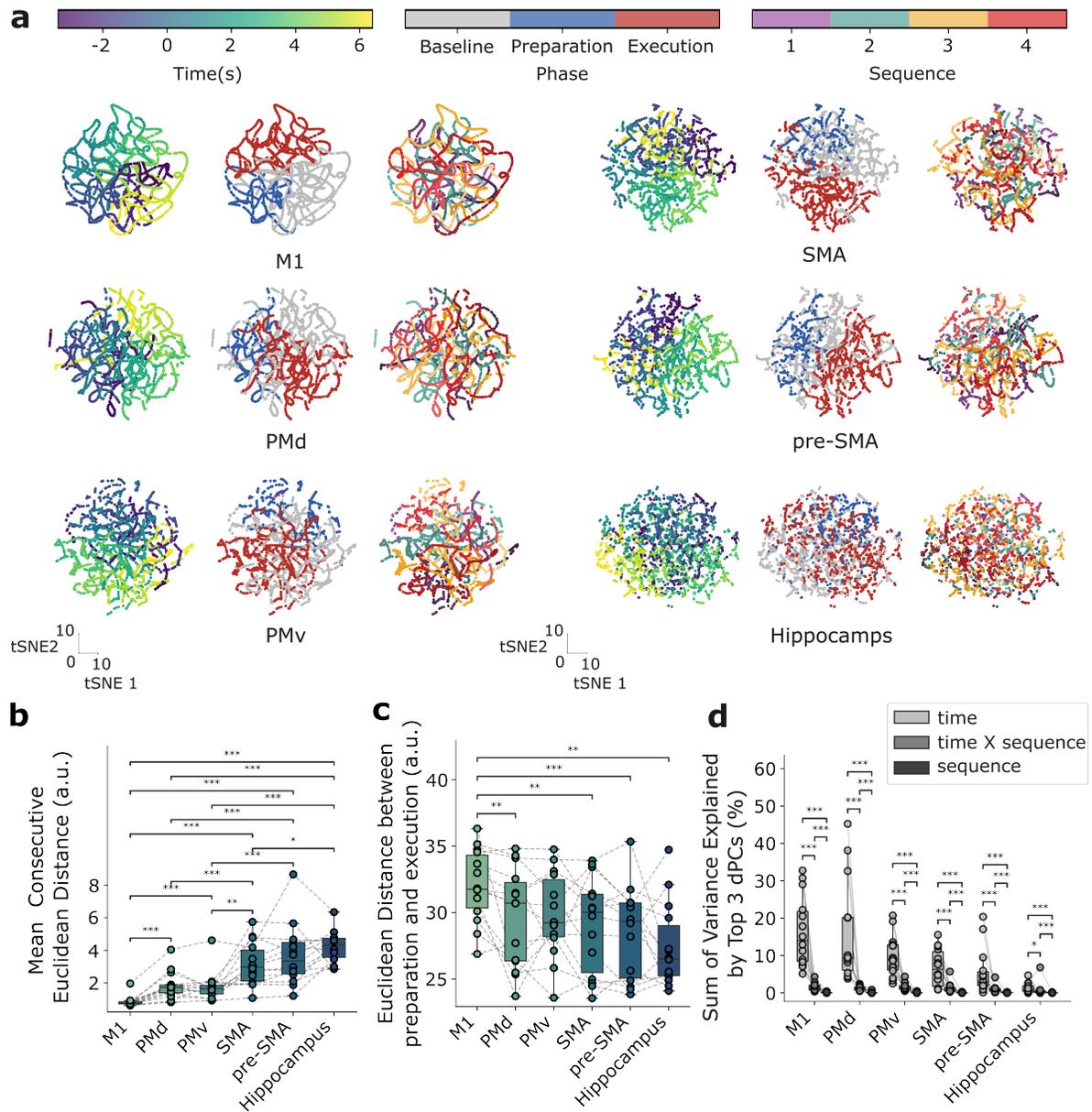
221 To extract the temporal evolution of high-dimensional covariance matrices, we used a sliding win-  
222 dow approach, which captures the internal functional connectivity or spatial coordination among  
223 local neural populations. These matrices were then embedded into a low-dimensional space by  
224 t-distributed Stochastic Neighbor Embedding (t-SNE), providing a sensitive probe of phase- and  
225 sequence-specific neural coding dynamics across brain regions during motor behaviour (Fig.4a).  
226 Critically, this analysis highlighted heterogeneity in how different brain regions traversed this phase  
227 transition: The primary motor cortex (M1) showed greatest temporal continuity reflected by the small-  
228 est consecutive distances (Fig.4b; M1:  $0.848 \pm 0.332$ ; PMd:  $1.839 \pm 0.845$ ; PMv:  $1.756 \pm 0.899$ ; SMA:  
229  $3.145 \pm 1.326$ ; pre-SMA:  $3.677 \pm 1.887$ ; Hippocampus:  $4.210 \pm 0.959$ ). In contrast, the hippocampus  
230 displayed a more scattered and discontinuous trajectory, indicating weaker internal organisation or  
231 sequential changes in local coordination relative to the task phases. A Friedman test confirmed robust  
232 regional differences in trajectory continuity ( $\chi^2(5) = 60.204$ ,  $p < .001$ ). Post-hoc Wilcoxon rank-sum  
233 tests with BH-FDR across 15 area pairs revealed significant distances among many regions (following  
234 pairs have  $p < .001$ : M1 vs. PMd, M1 vs. PMv, M1 vs. SMA, M1 vs. pre-SMA, M1 vs. hippocampus,  
235 PMd vs. SMA, PMd vs. pre-SMA, PMd vs. hippocampus; PMv vs. pre-SMA, PMv vs. hippocampus;  
236 other significant pairs: PMv vs. SMA:  $p = .003$ ; SMA vs. hippocampus:  $p = .021$ ).

237 Next, we quantified the distance between low dimensional phase clusters, which provides a mea-  
238 sure of preparatory-to-execution progression (Fig.4c; M1:  $32.02 \pm 2.73$ ; PMd:  $29.62 \pm 3.73$ ; PMv:  
239  $29.78 \pm 3.20$ ; SMA:  $29.06 \pm 3.61$ ; pre-SMA:  $28.52 \pm 3.45$ ; Hippocampus:  $27.41 \pm 3.16$ ). M1 showed  
240 significantly greater phase separation than other regions (Friedman test:  $\chi^2(5) = 16.490$ ,  $p = .006$ ;  
241 post-hoc Wilcoxon rank-sum tests, BH-FDR corrected over 15 comparisons: M1 vs. PMd:  $p = .009$ ;  
242 M1 vs. SMA:  $p = .025$ ; M1 vs. pre-SMA:  $p = .009$ ; M1 vs. Hippocampus:  $p = .009$ ), suggesting  
243 a structured, continuous remapping of spatial coding underlying motor control. This suggests that  
244 phase transitions are not merely governed by scaling a fixed pattern, but rely on gradual, structural

245 shifts in spatial neural coding.

246 To quantify this statistically, we sought to dissociate the variance arising from time-dependent  
247 changes, sequence identity by applying demixed principal component analysis (dPCA). This method  
248 extends PCA by constraining components to separately capture variance attributable to time, se-  
249 quence identity, or their interaction. The majority of variance was aligned with the temporal transition,  
250 with the hippocampus exhibiting the least variance and M1 showing the highest variance among mo-  
251 tor regions (Fig.4d; M1:  $16.37 \pm 9.37\%$ ; PMd:  $15.72 \pm 13.64\%$ ; PMv:  $9.70 \pm 5.55\%$ ; SMA:  $6.77 \pm 5.00\%$ ;  
252 pre-SMA:  $5.46 \pm 6.14\%$ ; Hippocampus:  $1.34 \pm 1.31\%$ ). In contrast, components specifically attributed  
253 to sequence identity accounted for only a small proportion of the total variance and showed weaker  
254 separability across sequences (Fig.4d; time x sequence: M1:  $1.65 \pm 1.04\%$ ; PMd:  $1.29 \pm 0.59\%$ ; PMv:  
255  $1.55 \pm 1.00\%$ ; SMA:  $1.26 \pm 1.41\%$ ; pre-SMA:  $0.99 \pm 0.97\%$ ; Hippocampus:  $0.76 \pm 1.76\%$ ; sequence:  
256 M1:  $0.11 \pm 0.12\%$ ; PMd:  $0.09 \pm 0.23\%$ ; PMv:  $0.11 \pm 0.13\%$ ; SMA:  $0.05 \pm 0.08\%$ ; pre-SMA:  $0.07 \pm 0.07\%$ ;  
257 Hippocampus:  $0.03 \pm 0.06\%$ ). Comparing different stimulus variance within the area showed signif-  
258 icance (Wilcoxon rank-sum tests, BH-FDR corrected over 3 x 6 comparisons;  $p < .001$  for all pairs  
259 except for hippocampus time versus time x sequence:  $p = .03$ ).

260 When comparing across areas, Pre-SMA and SMA showed lower explained variance by the se-  
261 quence X time and sequence components than M1 (sequence X time: Friedman test:  $\chi^2(5) = 27.88$ ,  
262  $p < .001$ ; Wilcoxon rank-sum test; BH-FDR corrected over 15 pairs: M1 vs. pre-SMA:  $p = .040$ , M1  
263 vs. Hippocampus:  $p = .040$ , PMd vs. Hippocampus:  $p = .042$ , PMv vs. Hippocampus:  $p = .040$ ,  
264 SMA vs. Hippocampus:  $p = .040$ , pre-SMA vs. Hippocampus:  $p = .040$ ), (sequence: Friedman test:  
265  $\chi^2(5) = 19.55$ ,  $p = .002$ ; Wilcoxon rank-sum test; BH-FDR corrected over 15 pairs: M1 vs. SMA:  
266  $p = .034$ , M1 vs. Hippocampus:  $p = .034$ , PMv vs. Hippocampus:  $p = .034$ ).



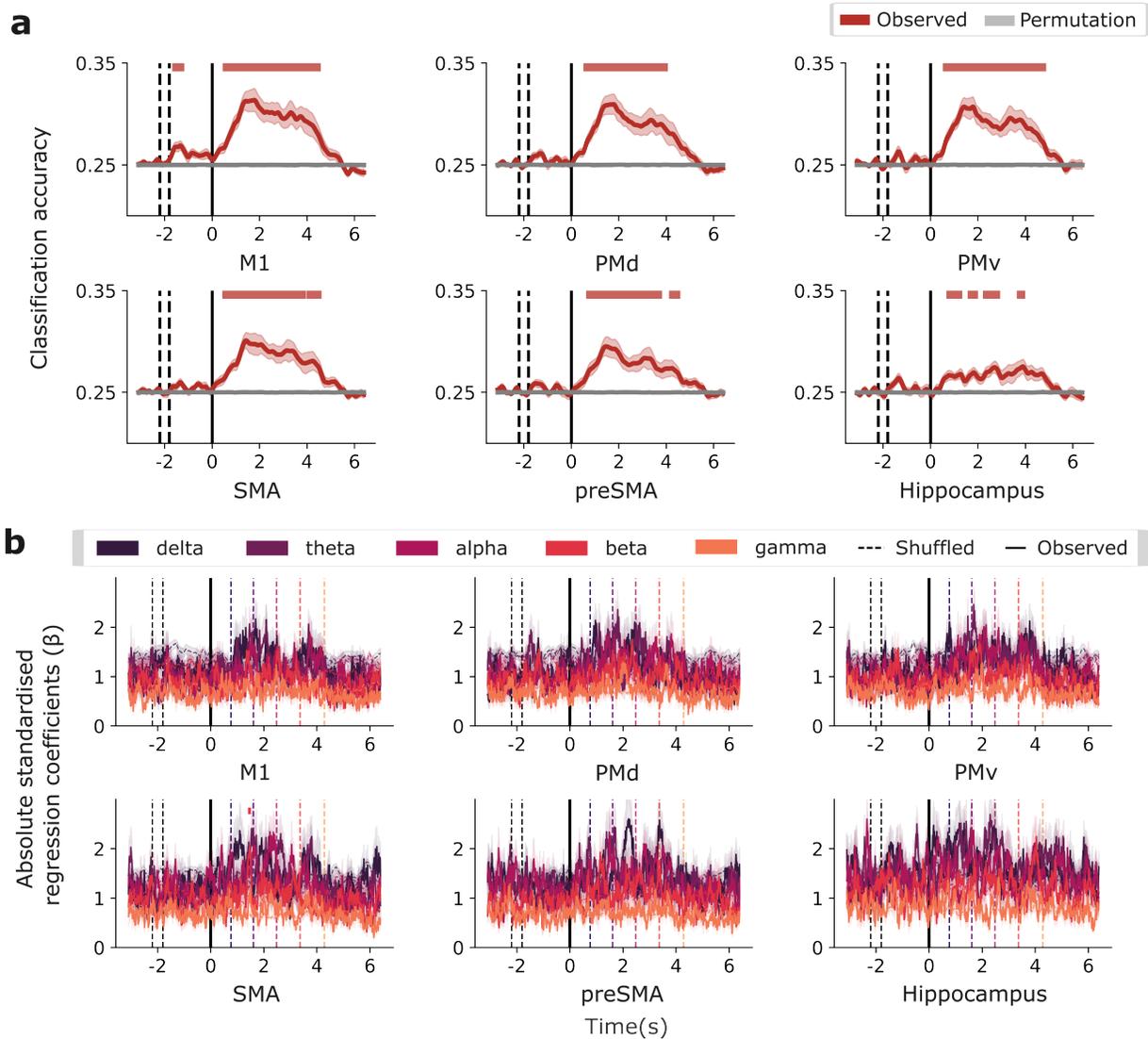
#### Figure 4: Time-resolved covariance structure reveals phase-specific clustering

(a) Example t-distributed Stochastic Neighbor Embedding (t-SNE) embedding of time-resolved covariance matrices six regions of interest (M1, PMd, PMv, SMA, pre-SMA, hippocampus). Covariance matrices were computed using 200Hz binned data with 200ms sliding window and 10ms stepsize and embedded into a 2D t-SNE space. Each subpanel consists of three small plots showing continuous time label (left), phase label (middle), sequence label (right). (b) Mean consecutive Euclidean distance between adjacent time points in the t-SNE space, averaged across participants. Smaller distances indicate smoother, more temporally continuous trajectories, whereas larger distances reflect discontinuous or irregular transitions. Horizontal brackets denote significant pairwise differences (Wilcoxon rank-sum test, BH-FDR corrected over 15 comparisons). (c) Euclidean distance between preparatory and execution clusters within the t-SNE embedding, quantifying phase separation in each region. M1 exhibits significantly greater separation than other regions, indicating a sharper transition between preparatory and execution states. Individual participant values are shown with paired lines. Horizontal brackets denote significant pairwise differences (Wilcoxon rank-sum test, BH-FDR corrected). (d) Variance explained by the top three demixed PCA (dPCA) components for each region, decomposed into contributions from time, sequence, and time  $\times$  sequence factors. Each dot represents one participant; boxplots show group distributions. Asterisks mark significant differences between component types within region (Wilcoxon signed-rank tests, BH-FDR corrected). (e) Time-resolved Euclidean distance between preparatory and execution covariance matrices, averaged across participants. Distances were computed in a sliding window aligned to key behavioural markers (Go cue: dashed lines; first movement: solid line). Shaded regions show SEM. Phase separation increases sharply after the Go cue, consistent with state transitions revealed in the t-SNE analysis.

## 267 2.5. Decoding sequence identity

268 Finally, we set out to test whether sequence-specific patterns, whilst distinct across phases, could be  
269 utilised to decode the sequence identity. We applied sliding window LDA, training and testing within  
270 the same peri-movement phase, to probe when sequence identity could be recovered during prepara-  
271 tion and production. (Fig.5a). Decoding accuracy significantly exceeded the shuffled baseline,  
272 primarily during execution in all motor regions, but not significantly in the hippocampus. M1 was the  
273 only region from which sequence identity could be reliably recovered during sequence preparation  
274 (-1.66 – 1.17 s).

275 To evaluate the spectral contributions to decoding, trial-wise LDA outputs were regressed onto  
276 z-scored power in canonical frequency bands (Fig. 5b). The resulting regression coefficients were  
277 temporally unstable, and most did not exceed significance relative to the shuffled correlation baseline,  
278 suggesting that no individual frequency band reliably drives sequence decoding.



**Figure 5: Sliding window decoding of sequence identity. (a)** Sliding window LDA decoding of sequence identity. A linear discriminant classifier was trained and tested within each time window (200 ms window, 10 ms step) to decode the four finger sequences. Red lines indicate subject averaged classification accuracy based on real labels; gray lines represent chance-level performance ( $n = 14$ ). Shaded red regions highlight time intervals where decoding exceeded shuffled baseline (cluster forming  $\alpha = .01$ , final cluster  $\alpha = .05$ ). All motor areas showed above-chance decoding during execution, with region-specific timing differences. The hippocampus exhibited lower decoding accuracy. **(b)** Regression coefficients relating frequency band power to decoder output. Colored lines represent the standardised correlation coefficient of delta (1–4 Hz), theta (4–8 Hz), alpha (8–13 Hz), beta (13–30 Hz), and gamma (30–80 Hz) bands. Colored shading at the top indicates time points with significant correlation relative to the shuffled regression null distribution (cluster forming  $\alpha = .01$ , final cluster  $\alpha = .05$ , Bonferroni-corrected across frequency bands).

### 279 **3. Discussion**

280 Invasive neural recordings in humans and non-human primates reveal a consistent computational  
281 principle during the peri-movement phase: cortical motor areas maintain orthogonal population dy-  
282 namics to functionally separate motor preparation from motor execution, preventing premature motor  
283 output [2–4, 29, 30]. Our MEG results in humans extend this notion beyond primarily motor regions  
284 in the context of the preparation and execution of movement sequences. We show that the neural ac-  
285 tivity underlying motor sequence preparation and execution from memory undergoes a pronounced  
286 global state shift prior to movement onset across motor, premotor, medial prefrontal and hippocam-  
287 pal regions previously shown to be involved in memory-guided motor sequence control [8, 9]. This  
288 fundamental geometric property of neural dynamics ensures the decoupling of planning and act-  
289 ing, whether the motor output is a discrete single action or part of a complex, memory-retrieved  
290 behavioural sequence.

#### 291 **Hierarchical transition to execution patterns**

292 Across all regions of interest, the termination of preparatory patterns occurred largely synchronously  
293 after the Go Cue, suggesting a global, externally driven reset - here by a visual Go Cue stimulus -  
294 propagating to multiple nodes in the network. In contrast, execution-related sequence patterns did  
295 not unfold simultaneously. Instead, their onset varied systematically across regions, consistent with a  
296 hierarchical organisation and the regions' proximity to the periphery (M1 and motor units in the spinal  
297 chord) [28]. In the hippocampus, pre-SMA, and SMA, the shift towards execution patterns appeared  
298 ~600 ms or more and ~400 ms before the first button press, whereas in M1, an area closer to the  
299 periphery due to dense cortico-spinal outputs, the shift emerged only ~100 ms before finger press  
300 onset. Although this temporal ordering aligns with a top-down progression from higher- to lower-  
301 level motor-related areas close to the periphery, the ~500 ms delay between the state changes in  
302 pre-SMA and M1 cannot be explained by direct cortico-cortical interactions. This points towards an  
303 iterative involvement of subcortical, likely striato-thalamo-cortical loops in triggering state-changes  
304 across brain regions [31].

305 Despite evidence for hierarchically timed transitions to execution states, we observed substantial  
306 inter-individual variability in the timing of these transitions, particularly in premotor areas and the  
307 hippocampus, with some participants showing state transitions to execution driven patterns even  
308 before the Go Cue onset. This could reflect differences in task strategy, such as different offsets of  
309 abstract sequential cognitive planning versus onsets of lower-level kinaesthetic motor imagery when  
310 motor sequences are retrieved from memory and prepared for execution, albeit in the absence of  
311 movement.

312 Across primary motor and premotor cortices, the oscillatory signatures underlying this state tran-  
313 sition were not confined to a single frequency band modulation observed during motor preparation  
314 and production, such as beta or alpha, but were instead broadband. In contrast, the hippocampus  
315 exhibited a band-specific profile, relying primarily on theta activity to predict the transition. Motor state  
316 transitions from preparation to execution recruit multiple physiological processes, such as the release  
317 of inhibition reflected in beta activity, increases in excitability indexed by alpha ( $\mu$ ) desynchronisa-  
318 tion over motor areas [13, 32], and local processing often associated with higher-frequency activity  
319 resulting in broadband spectral changes [33]. The hippocampus, in contrast, supports sequence re-  
320 trieval, and memory-guided planning, functions tightly coupled to theta oscillations. Theta organises  
321 hippocampal firing sequences (phase precession, theta sequences) [34] and is the dominant rhythm

322 for these computations. In contrast, hippocampal state transitions are predominantly mediated by  
323 theta-dependent phase coding, which is sufficient to represent shifts between mnemonic or planning  
324 states [35].

### 325 **Sequence representations are phase-dependent and dynamic**

326 Whilst the neurophysiological patterns associated with sequence preparation and execution occu-  
327 pied distinct subspaces, suggesting limited overlap in sequence tuning, they were not completely  
328 orthogonal and showed significant covariance. This residual overlap suggests that preparing an  
329 entire movement sequence inherently recruits components of the execution-related representation.  
330 Notably, this stands in contrast to prior findings in single-movement tasks, where preparatory and  
331 execution states have been shown to be more cleanly dissociable [3]. One possibility is that motor  
332 sequence preparation engages processes akin to motor imagery, whereby aspects of the upcoming  
333 movements are internally simulated before execution. Such internal simulation — particularly in the  
334 form of kinaesthetic motor imagery [36] — could account for the partial overlap observed between  
335 preparatory and execution-related neural states. This overlap may be related to the lack of sequential  
336 movement fusion, as the presses, although well-trained were not retrieved as one holistic movement,  
337 but as a concatenation of kinematically discrete elements [37, 38].

338 Neural patterns related the trial phase before and after movement onset accounted for the largest  
339 portion of variance in MEG dynamics (dPCA), whereas time and sequence identity had a smaller  
340 influence. Notably, whole-sequence patterns did not generalise across the perimovement phase, in-  
341 dicating that sequence-specific coding changes dynamically between motor sequence preparation  
342 and execution. In other words, activity does not occur in a separate “space” for each sequence and  
343 evolves collectively before and after movement onset, yet each sequence retains its own distinctive  
344 trajectory within those subspaces. The most pronounced distance between sequences unfolds in the  
345 execution phase when movements diverge in their identity and timing after the first press for execu-  
346 tion. The trajectories exhibited regional differences in continuity with more smoothness in M1 versus  
347 upstream motor regions. This echoes invasively recorded population pattern trajectories recorded in  
348 the context of sequential motor control in non-human primate M1 versus SMA [29].

349 Although the sequential code was subtle and highly dynamic, MEG patterns still allowed reliable  
350 decoding of the press sequences during execution across all motor areas and even before movement  
351 onset in M1. While decoding accuracy was modest and far from sufficient for non-invasive BCI  
352 applications, it is nevertheless striking that sequential information can be extracted from non-invasive  
353 MEG dynamics, given how similar the finger press sequences were: they involved the same digits,  
354 half involving the same digit order paired with the different temporal structure, the same number of  
355 presses and an identical first digit across sequences within each sequence set per participant. Unlike  
356 previous single-cell and fMRI studies reporting premotor tuning to full movement sequences during  
357 preparation [8, 20, 39, 40], we found above-chance decoding during preparation confined to M1, with  
358 widespread decoding only during execution — a discrepancy that could be resolved via cross-modal  
359 fusion analyses [41].

360 Although decoding accuracy in both preparation and production was found to be related to power  
361 changes across multiple oscillatory frequencies, these frequency power modulations explained only  
362 up to three percent of the decoding accuracy, suggesting that sequence content is not driven by  
363 simple global markers in neuronal excitation and inhibition, such as beta event-related desynchroni-  
364 sation or rebound, e.g. in motor areas. This suggests power alone is not the main driver of decoding;  
365 instead, richer phase dynamics encode sequence information.

## 366 **Recovering motor dynamics from non-invasive brain activity**

367 How can this state shift be picked up with non-invasive recordings such as MEG? While both MEG  
368 and invasive electrode arrays offer high temporal resolution, they differ in the types of signals they  
369 capture. MEG records extracellular magnetic fields generated by synchronised neuronal currents  
370 across large populations of pyramidal neurones [42], whereas microelectrode arrays primarily detect  
371 the spiking activity of individual neurones near the electrodes. MEG signals diminish with distance  
372 from the source and are especially sensitive to superficial cortical activity [43], whereas invasive  
373 electrodes can access deeper layers and brain regions. MEG thus reflects population-level brain  
374 oscillations and pre-synaptic neural processing in a brain area. Despite these differences, the overall  
375 population-level dynamics successfully capture neural dynamics the major state transitions between  
376 movement preparation and execution. This suggests that aspects of internal neural dynamics can  
377 be inferred through non-invasive population-level measurements, even in the presence of reduced  
378 spatial precision. Non-invasive recordings such as MEG — and, moving forward, OPM-MEG [44] —  
379 combined with source reconstruction of individual brain regions, can simultaneously capture activity  
380 across multiple areas. This capability is increasingly recognised as critical for BCI development, as  
381 focusing solely on M1 overlooks the contributions of a broader network of regions. Accessing signals  
382 from multiple areas could provide additional information to improve BCIs' ability to interpret the user's  
383 intent [39, 45, 46].

## 384 **Conclusions**

385 In sum, we show that motor sequence preparation and execution involve a global state shift across  
386 motor, premotor and hippocampal regions, unfolding hierarchically between areas removed from the  
387 periphery to those with dense cortico-spinal connections. Preparatory and execution-related patterns  
388 are largely distinct but partially overlapping, consistent with internal simulation or motor imagery of  
389 upcoming sequences. Sequence-specific information is subtle, dynamic, and distributed across mul-  
390 tiple frequencies and phases, emerging most strongly during execution but detectable even before  
391 movement onset. Critically, non-invasive MEG captures these population-level dynamics, highlight-  
392 ing both fundamental principles of hierarchical motor control and their relevance for brain-computer  
393 interfaces, where monitoring multiple regions beyond M1 could enhance decoding of user intent.

## 394 4. Methods

### 395 4.1. Memory-guided finger sequence task

396 This study reanalysed MEG data from Kornysheva et al. (2019) [25]. Of the original 16 healthy right-  
397 handed participants, 14 were included in the analysis: one was excluded due to motion artefacts,  
398 another due to imbalance in sequence accuracy across finger sequences. Participants were trained  
399 over two days to associate four abstract visual cues with four five-finger tapping sequences, drawn  
400 from a pool of 16 fractal images. Each sequence combined one of two finger orders (F1, F2) with  
401 one of two temporal interval orders (T1, T2; 550, 650, 800, 983, and 1300 ms), yielding a  $2 \times 2$   
402 factorial design. For each participant, the identity of the first finger press remained constant across  
403 all four sequences. On the third day, participants viewed a visual sequence cue followed by a vari-  
404 able delay (1.8, 2.0, or 2.2 s) and then initiated the memorised sequence upon the Go Cue. Each  
405 sequence was presented in groups of three consecutive repetitions, with the order of the groups ran-  
406 domised across the session, for a total of 60 repetitions per sequence. MEG data were continuously  
407 recorded at 1200 Hz using a 275-channel axial gradiometer system (CTF Omega, VSM MedTech)  
408 in a magnetically shielded room. As in the original study, sensor-level data were preprocessed us-  
409 ing Independent Component Analysis (ICA) to remove artefacts and downsampled to 1000 Hz. Trial  
410 segments spanned from  $-2.8$  s before to 12 s after sequence cue onset. Only correctly performed  
411 trials were included in the analysis, defined by the accurate finger press order and timing within the  
412 specified interval windows.

### 413 4.2. Statistics analysis

414 Statistical analyses were performed using non-parametric methods. Group-level omnibus effects  
415 were assessed using the Friedman test. Pairwise comparisons were conducted using Wilcoxon  
416 signed-rank tests. One-sample comparisons against reference values were performed using one-  
417 sample Wilcoxon signed-rank tests. The family-wise error rate was controlled using the Bonferroni  
418 correction for fewer than 10 comparisons, and the false discovery rate Benjamini–Hochberg (FDR-  
419 BH) procedure for ten or more comparisons. Time-resolved statistics were evaluated using cluster-  
420 based permutation testing with a cluster-forming threshold of  $p < .01$ , and clusters were deemed  
421 significant at  $p < .05$  with false discovery rate correction.

### 422 4.3. MEG source reconstruction

423 Sensor data were co-registered to a template MRI using fiducial-based alignment in FieldTrip (<http://www.fieldtriptoolbox.org/>, v20241025), based on the nasion and left/right preauricular points.  
424 A single-shell volume conduction model was used to compute the leadfield matrix, with grid points  
425 defined at 1 cm resolution. Source reconstruction was performed with a linearly constrained minimum  
426 variance (LCMV) beamformer. Sensor data were baseline-demeaned using the 1 s interval preceding  
427 the sequence cue. A common spatial filter was computed per subject using the whole-trial (14s)  
428 covariance matrix, averaged across all correct trials to ensure consistent source orientation.

429 Motor regions (M1, SMA, pre-SMA, PMd, PMv) were defined using the atlas [47], and the hip-  
430 pocampus using NeuroVault masks [48]. Grid points belonging to each ROI were identified by  
431 anatomical labels and aggregated by region. Source time series were extracted at full temporal  
432 resolution (1000 Hz). The source channels were sorted and filtered using the anatomical coordinates  
433 to ensure consistent and comparable source channels across subjects.  
434

#### 435 **4.4. Time frequency analysis and cluster-based statistical testing**

436 Time–frequency representations (TFRs) were computed from the source-localised data (1000Hz)  
437 using the multitaper method. Data were aligned to the Go Cue without truncation and mirror-padded  
438 to 40 s to prevent edge artefacts. Spectrum power was estimated from 0.5 to 80 Hz in 0.5 Hz step  
439 and 50 ms timestep. Hanning taper with a window length of six cycles per frequency were applied.

440 For visualisation, TFRs were dB-normalised relative to 1 s baseline period prior to Go Cue individ-  
441 ually and then grand-averaged across participants. Group-level baseline demeaning was performed  
442 to centre baseline grand-average activity to zero.

443 Statistical evaluation of task-related power changes was performed using a cluster-based permu-  
444 tation test (FieldTrip function `ft_freqstatistics`). The 1 s baseline period was repeated to match  
445 the task window length. Significance was assessed using a Monte Carlo method with dependent-  
446 samples t-statistics (`cfg.method = 'montecarlo'`, `cfg.statistic = 'depsamplesT'`, `cfg.correctm = 'cluster'`).  
447 The cluster-forming threshold was set at `clusteralpha = .01`, and post-permutation clusters were con-  
448 sidered significant at `alpha = .05`.

#### 449 **4.5. Linear discriminant analysis on phase prediction**

450 Linear Discriminant Analysis (LDA) was applied to source-reconstructed time series, downsampled  
451 to 200 Hz. For each participant, the classifier was trained to discriminate between eight conditions  
452 defined by a  $2 \times 4$  factorial design: task phase (preparation vs execution) crossed with sequence  
453 identity (sequences 1–4). This yielded the following labels: `prep×seq1`, `exec×seq1`, ..., `prep×seq4`,  
454 `exec×seq4`. The preparation period was defined from sequence cue onset to the variable Go Cue;  
455 execution spanned from the first to the final finger press, defined based on trial-wise variable timing.

456 Decoding results were averaged across 1,000 bootstraps. For each iteration, 40 correctly per-  
457 formed trials were sampled per sequence (or the maximum number of available trials if fewer; only  
458 participant had fewer trials than 40 trials for one sequence) and split into training and test sets (70/30  
459 ratio), with stratification to maintain sequence balance. Samples equivalent of 1 s length was ran-  
460 domly extracted from either the preparation or execution period of each training trial and labelled by  
461 phase–sequence identity. The trained classifier was then applied continuously to the full test-trial  
462 time course to obtain decoding probability trajectories.

463 Chance level baselines were generated by repeating this procedure with randomly permuted class  
464 labels while controlling all other processing steps constant. Classification accuracy values represent  
465 the time-resolved accuracy of assigning the correct phase–sequence label, calculated exclusively  
466 from test trials of the matching sequence. For visualisation, accuracy curves were first averaged  
467 across repeats within participants, then aggregated mean and standard error (SEM) across par-  
468 ticipants. The cluster-based permutation test performed across observed and permuted decoding  
469 curves (`clusteralpha = .01`, final cluster `alpha = .05`, Bonferroni-correction over 2 phases).

470 To quantify the timing of phase transitions, decoding curves were aligned to task events to account  
471 for the variable Go Cue and press timing. Go Cue aligned prediction curves were used to measure the  
472 offset of preparation patterns and first press alignment for the onset of execution patterns. Cluster-  
473 based permutation significance is computed per participant using the 1,000 bootstraps of observed  
474 trials and permutation probability (`clusteralpha = .01`, final cluster `alpha = .05`, Bonferroni-correction  
475 over 2 phases). Significant clusters shorter than 10 ms were discarded, and clusters separated by  
476 less than 10 ms were merged before extracting timing estimates.

#### 477 **4.5.1. Linear mixed-effects models testing hierarchical trend in transition timings**

478 To test whether the timing of neural state transitions followed the assumed cortical–hippocampal  
479 hierarchy, we defined the ordinal rank of regions with the reported anatomical density of direct cortico-  
480 spinal projections to the lower cervical segments of the spinal cord (C7–T1) and cortico-cortical  
481 connectivity to M1: Hippocampus (Rank = 1), pre-SMA(Rank = 2), SMA(Rank = 3), PMv(Rank = 4),  
482 PMd(Rank = 5) and M1(Rank = 6).

483 For each transition type, we fitted a linear mixed-effects model of the form:

$$\text{Transition Time}_{ij} = \beta_0 + \beta_1 \text{Rank}_{ij} + u_{0j} + \varepsilon_{ij},$$

484 where  $\beta_0$  is the intercept,  $\beta_1$  indexes the linear trend across the hierarchical axis,  $u_{0j}$  is a random  
485 intercept for subject  $j$ , and  $\varepsilon_{ij}$  is residual error.

486 A negative  $\beta_1$  indicates progressively earlier transitions toward M1 (hippocampus  $\rightarrow$  M1), whereas  
487 a positive  $\beta_1$  reflects the opposite trend. Standardised coefficients were computed to provide an in-  
488 terpretable effect size:

$$\beta_1^* = \beta_1 \times \left( \frac{\text{SD}(\text{Rank})}{\text{SD}(\text{Transition Time})} \right),$$

489 representing the change in onset time (in SD units) per SD change in region rank.

490 Two-tailed tests were performed for  $\beta_1$  ( $H_0 : \beta_1 = 0$ ), with significance defined as  $\alpha = 0.05$ .

#### 491 **4.6. Regression of canonical frequency power onto LDA-derived state estimates**

492 To relate frequency-specific neural activity to the emergence of preparation and execution patterns,  
493 LDA predictions were regressed against canonical frequency band power. Time–frequency repre-  
494 sentations (TFRs) were computed for each participant using the same setting as above, but at high  
495 temporal resolution (200 Hz) to match both the sampling rate and temporal structure of the LDA  
496 output. Spectral power was extracted for five canonical frequency bands: delta (1 – 4Hz), theta  
497 (4 – 8Hz), alpha (8 – 13Hz), beta (13 – 30Hz), and gamma (30 – 80Hz). TFRs were z-scored per  
498 trial and then averaged across trials within each sequence and frequency band.

499 To examine the relationship between spectral dynamics and execution-related decoding, LDA pre-  
500 dictions were z-scored then averaged across 1,000 bootstrap repeats per sequence. Time-resolved  
501 correlations were computed using a sliding window approach at 200 ms window and 10 ms step.  
502 For each window, a predictor matrix  $X \in \mathbb{R}^{160 \times 5}$  (4 sequences  $\times$  40 timepoints  $\times$  5 bands) was  
503 regressed against the corresponding LDA predictions  $y \in \mathbb{R}^{160}$  (4 sequences  $\times$  40 timepoints) using  
504 ridge regression with a regularisation parameter of  $\alpha = 1$ .

505 Statistical significance was assessed using the cluster based permutation test against the per-  
506 muted correlation curve (cluster-forming alpha = .05; corrected alpha = .01, Bonferroni-corrected over  
507 5 frequencies). The permutation correlation curve was generated by circularly shifting the predictor  
508 time series with a minimum shift of 10% of the trial time length across 1000 repeats.

509 A similar analysis was performed to assess the relationship between spectral dynamics and se-  
510 quence identity predictions. In this case, the LDA classifier already yielded time-resolved sequence  
511 predictions using the same sliding-window configuration (200 ms window, 10 ms step). The spectral  
512 predictors were temporally aligned to the corresponding LDA output for each window. The predictors  
513 were z-scored along the time dimension, and ridge regression ( $\alpha = 1$ ) was applied at each time win-  
514 dow. Statistical assessment followed the same permutation framework as described above. For each  
515 participant, a null distribution of regression coefficients was generated by 1000 repeats of circularly  
516 shifting the LDA prediction time windows.

## 517 **4.7. Principal component analysis**

518 Principal component analysis (PCA) was performed separately for each participant using source-  
519 reconstructed data binned at 200 Hz. The dimensionality of the data was reduced to the first 10  
520 principal components (PCs), or to the minimum number of available source channels if fewer than  
521 10. For visualisation, PCA-transformed time series were averaged across trials for each sequence  
522 condition and smoothed using a one-dimensional Gaussian filter ( $\sigma = 25$  ms).

### 523 **4.7.1. Kolmogorov–Smirnov distance**

524 To quantify separation between preparation and execution activity along each principal component,  
525 the Kolmogorov–Smirnov (KS) distance was computed between their respective distributions. To  
526 account for unequal sample sizes, 1 000 bootstrap iterations were performed in which 500 time points  
527 were randomly drawn from each phase. The null distribution was constructed by repeating the same  
528 procedural with randomly permuted phase labels. KS distances were averaged across bootstrap  
529 repetitions for each participant, and group-level differences between observed and null values were  
530 assessed using paired Wilcoxon signed-rank tests, FDR-BH over 3 PCs x 6 areas.

531 Separation between preparatory and execution states was quantified as the mean Euclidean dis-  
532 tance between execution-phase points and the preparatory centroid:

$$D_{exec \rightarrow prep} = \frac{1}{n} \sum_{i=1}^n \left\| \mathbf{x}_i - \boldsymbol{\mu}_{prep} \right\|_2, \quad \text{where } \boldsymbol{\mu}_{prep} = \frac{1}{m} \sum_{j=1}^m \mathbf{y}_j$$

533 Distance per participant were obtained using bootstrap resampling (1,000 iterations; 500 samples  
534 per phase) with an identical phase-shuffled permutation procedure to generate a null distribution.  
535 Group-level effects were assessed using paired Wilcoxon signed-rank tests with FDR correction.

### 536 **4.7.2. Alignment index**

537 To assess the alignment of subspaces between preparatory and execution dynamics [49], separate  
538 principal component analyses (PCA) were performed on data corresponding to the preparation (prep-  
539 PCA) and execution phases(execPCA).

$$\text{Alignment} = \frac{1}{k} \text{Tr} \left( U_{exec}^\top P_{prep} U_{exec} \right) = \frac{1}{k} \text{Tr} \left( U_{exec}^\top U_{prep} U_{prep}^\top U_{exec} \right).$$

540 where  $U_{prep}$  and  $U_{exec}$  are the PCA basis matrices (with orthonormal columns) for the preparatory  
541 and execution subspaces, respectively, and  $P_{prep} = U_{prep} U_{prep}^\top$  is the projection operator onto the  
542 preparatory subspace. The alignment index measures the extent to which the execution components  
543 lie within the preparatory subspace. A value of 1 indicates perfect alignment, while lower values  
544 indicate greater orthogonality. Statistical significance was assessed by comparing the alignment  
545 index against 1 using a one-sample Wilcoxon signed-rank tests

### 546 **4.7.3. Gaussian mixture model and rotation angle**

547 The angle between preparatory and execution states was quantified in low-dimensional PCA space.  
548 For each participant and each brain region, a one-component Gaussian mixture model was fitted

549 separately to preparation and execution distributions derived from the first three PCs of the sequence-  
550 averaged embeddings. The principal direction of each state was defined as the eigenvector associ-  
551 ated with the largest eigenvalue of the fitted covariance matrix. Eigenvectors were sign-aligned by  
552 enforcing a positive first component to ensure directional consistency across states and subjects.

553 Angles between states were computed using the dot-product-based acute angle measure:

$$\theta = \arccos(|\mathbf{v}_{prep} \cdot \mathbf{v}_{exec}|)$$

554 yielding distances constrained to the range  $0^\circ - 90^\circ$ . For each region, one-sample Wilcoxon signed-  
555 rank tests were used to assess whether preparation - execution angles differed from no rotation ( $0^\circ$ )  
556 and orthogonality ( $90^\circ$ ) (Bonferroni correction over 6 areas).

#### 557 **4.8. Covariance matrix and t-distributed stochastic neighbour**

558 To visualise temporal changes in covariance structure, we performed a sliding-window covariance  
559 analysis on data downsampled to 200 Hz, using a 200 ms window and a 10 ms step. For each partic-  
560 ipant, covariance matrices were computed across trials and averaged within each sequence without  
561 further preprocessing. The resulting covariance matrices were then vectorised and embedded into  
562 a low-dimensional space using t-distributed stochastic neighbour embedding (t-SNE) (perplexity=5,  
563 ndim = 3).

564 Two summary measures were derived from the embedded covariance trajectories. The mean  
565 consecutive euclidean distance was computed by taking the Euclidean distance between succes-  
566 sive sequence-averaged embeddings in the 3-dimensional space. The euclidean distance between  
567 preparation and execution phases was quantified using a bootstrap (1000 repeats): in each iteration,  
568 an equal number of samples per phase ( $N = 500$ ) was drawn, and the Euclidean distance between  
569 the execution-state points and the centroid of the preparation-state points was calculated.

##### 570 **4.8.1. Correlation distance between phases**

571 To quantify similarity in covariance structure between preparatory and execution periods, trial-wise  
572 covariance matrices were first labelled and grouped according to phase identity. Similarity was esti-  
573 mated using a bootstrap procedure applied separately for each participant. In each iteration, 10,000  
574 bootstrap samples were drawn from each phase and averaged, and covariance similarity was quan-  
575 tified using correlation distance:

$$d = 1 - \text{corr}(\text{vec}(C_{prep}), \text{vec}(C_{exec})),$$

576 where  $C_{prep}$  and  $C_{exec}$  denote the averaged covariance matrices for the preparatory and execu-  
577 tion states, respectively, and  $\text{vec}(\cdot)$  refers to vectorisation of the upper triangular matrix excluding the  
578 diagonal. A null distribution was generated by repeating the full procedure after randomly permut-  
579 ing phase labels, thereby removing the systematic preparatory-execution structure while preserving  
580 covariance magnitude and sampling statistics.

#### 581 **4.9. Demixed PCA**

582 Demixed principal component analysis (dPCA) was applied to separate sources of variance at-  
583 tributable to time, sequence identity, and their interaction within the 200 Hz source-reconstructed  
584 time series [50]. For each participant and each brain region, dPCA was performed on correct trials,

585 using the minimum number of correct trials available across sequences to ensure balanced input. The  
586 dPCA input had dimensionality  $n_{\text{sequence}} \times n_{\text{repeats}} \times n_{\text{time}}$ , and the decomposition yielded three sets  
587 of principal components corresponding to the *time*, *sequence*, and *time*  $\times$  *sequence* marginaliza-  
588 tions. For each marginalisation, explained variance was quantified and the variance of the top three  
589 components was summed. To quantify separability between sequences in the source  $\times$  time compo-  
590 nent space, a sliding-window analysis (200 ms window, 10 ms step) was applied to compute pairwise  
591 Euclidean distances between sequence centroids at each time point. The resulting distances were  
592 then averaged across all pairwise comparisons to yield a summary measure of sequence separation.

#### 593 **4.10. Sliding window LDA for sequence decoding**

594 Sliding-window linear discriminant analysis (LDA) was performed using a 200 ms window with a 10  
595 ms step size on the 200 Hz source-level time series. For each subject, 40 correct trials per sequence  
596 were randomly sampled without replacement, and data were split into training and test sets using a  
597 70/30 stratified split. Within each time window, the LDA classifier was trained on the corresponding  
598 training-set segment and evaluated on the matching held-out test segment. Decoding accuracy was  
599 computed as the proportion of correctly classified test-set samples and then averaged across all time  
600 points within the window.

601 This sampling and decoding procedure was repeated 500 times per participants to estimate robust  
602 average decoding performance. Final accuracy time courses were obtained by averaging across  
603 repetitions. No temporal smoothing was applied. All analyses were performed independently for  
604 each brain region.

605 Statistical significance was assessed using a cluster-based permutation test relative to the per-  
606 muted baseline (cluster forming threshold = .01, cluster-level significance = .05). For each participant,  
607 a null distribution was generated by repeating the decoding procedure with randomly permuted se-  
608 quence labels (500 permutations). Observed decoding accuracy was then compared against this null  
609 distribution to determine whether performance exceeded chance.

#### 610 **4.11. Ethical Statement**

611 In the original study [25], all participants gave written informed consent to participate. The study was  
612 approved by the University College London Research Ethics Committee for Human-Based Research  
613 (UCL Ethics ID: 1338/006, Data Protection: Z6364106/2011/10/25). All participants were financially  
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