

## Cognitive strategies shift information from single neurons to populations in prefrontal cortex

### Highlights

- Sequencing strategies improve performance in a self-ordered working memory task
- Strategies distribute information from tuned LPFC neurons to population codes
- Less routine behavior and higher memory loads increase neural dimensionality

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### In brief

Strategies are commonly used to improve working memory performance, but whether they change the information held in mind is less clear. Using a self-ordered selection task, Chiang et al. show that adopting sequencing strategies shifts information from single, highly tuned neurons to more distributed population codes in lateral prefrontal cortex.



## Article

# Cognitive strategies shift information from single neurons to populations in prefrontal cortex

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## SUMMARY

Neurons in primate lateral prefrontal cortex (LPFC) play a critical role in working memory (WM) and cognitive strategies. Consistent with adaptive coding models, responses of these neurons are not fixed but flexibly adjust on the basis of cognitive demands. However, little is known about how these adjustments affect population codes. Here, we investigated ensemble coding in LPFC while monkeys implemented different strategies in a WM task. Although single neurons were less tuned when monkeys used more stereotyped strategies, task information could still be accurately decoded from neural populations. This was due to changes in population codes that distributed information among a greater number of neurons, each contributing less to the overall population. Moreover, this shift occurred for task-relevant, but not irrelevant, information. These results demonstrate that cognitive strategies that impose structure on information held in mind rearrange population codes in LPFC, such that information becomes more distributed among neurons in an ensemble.

## INTRODUCTION

Higher order cognitive abilities like planning and problem solving require online organization of information. This includes cognitive strategies that impose structure on information held in mind, such as creating lists or categories. For example, servers in a restaurant might remember customers' drink orders in a sequence so they can serve the right drink to the right person later on (Ericsson and Kintsch, 1995). Organizing information in this way allows us to overcome natural constraints on the capacity of working memory (WM). WM is the ability to hold information temporarily in mind, allowing it to be manipulated for cognitive processes (D'Esposito and Postle, 2015; Miller, 1956), but is restricted to approximately four units of stored information (Cowan, 2001; Luck and Vogel, 1997). Both WM and implementing cognitive strategies are well known to rely on intact function of the dorsolateral prefrontal cortex (dlPFC) (Bor et al., 2003; Miller, 2000; Nichelli et al., 1994), but the neural mechanisms that organize WM information online are not well understood. This is in part because it is challenging to capture the flexible, self-generated aspects of cognitive strategies that are most dependent on prefrontal function.

Strategies are deployed in many cognitive tasks, and a hallmark of prefrontal cortex function is flexible neural responses

that adapt to encode relevant information under varying task demands (Duncan, 2001). Indeed, at the single-neuron level, the selectivity of prefrontal neurons is not fixed but changes depending on the task being performed (Asaad et al., 1998, 2000; Funahashi et al., 1989; Rao et al., 1997). Dynamic coding is also observed at the population level in prefrontal cortex (Meyers, 2018; Rigotti et al., 2013; Sigala et al., 2008; Stokes et al., 2013), but how this relates to changing task demands and single-unit selectivity is not well understood. In some cases, it has been found that task information can be decoded from subsets of prefrontal ensembles as reliably as from the whole population (Leavitt et al., 2017; Meyers et al., 2008), suggesting that neurons provide either unequal or redundant contributions to the overall population code. More recently, empirical (Bartolo et al., 2020) and theoretical (Gao et al., 2017) approaches have shown low dimensionality of population activity obtained from large-scale recordings, suggesting constraints on the diversity of activity patterns generated by a population of neurons. However, to date, it remains unclear how these properties of population activity relate to adaptive coding commonly observed in prefrontal cortex. One possibility is that the flexible changes in single neuron responses are part of larger changes in neuronal ensembles that optimize population coding under different cognitive demands. Here, we investigated this in a WM task, by examining



how ensemble encoding changes when subjects use strategies that impose structure on mnemonic information, thus changing the cognitive demands of the task.

Recently, we found that monkeys spontaneously adopt sequencing strategies in a spatial self-ordered target selection task that taxes their WM capacity (Chiang and Wallis, 2018b). Despite improved task performance, the strength of spatiotemporal tuning among neurons in the lateral prefrontal cortex (LPFC) decreased with more sequential behavior. Given the involvement of prefrontal cortex in strategy implementation, the apparent loss of information from LPFC is not intuitive. To assess how changes in single-unit selectivity contribute to ensemble coding under different cognitive demands, we decoded task information, including target locations, orders, and colors, from ensembles of LPFC neurons. We found that even though the individual neurons were less tuned, the accuracy of decoding task-relevant information remained the same or increased when subjects performed more sequenced selection patterns. Further analyses revealed that the sizes of the neural ensembles that yielded optimal decoding increased with sequencing strategies, suggesting that information became more distributed within the population, but less efficiently coded at a single-neuron level. Last, behavior that was less stereotyped led to more diverse activity patterns, with higher dimensionality. Together, these results demonstrate that using a cognitive strategy to structure behavior systematically changes neural codes in LPFC, shifting information from single, highly tuned neurons to populations. This additionally suggests that online adaptations of population-level codes may underlie flexible cognitive abilities.

## RESULTS

### Single-neuron spatial tuning is modified by self-ordered search strategies

When faced with a task that exceeds the capacity limits of WM, humans and animals tend to use mnemonic strategies. For animals, we operationally define “strategies” as patterns of behavior that indicate a superordinate organization, which may or may not be deliberately selected by the subject. For instance, a previous study showed that monkeys spontaneously adopted sequencing strategies to accomplish a target selection task that required them to track the self-ordered selections of six identical visual targets (Chiang and Wallis, 2018b). In the task, two monkeys were presented with spatial configurations of targets, represented by colored circles on a computer screen. Starting from a central fixation point, they had to saccade to one target at a time to obtain a juice reward and then return gaze to fixation before the next selections (Figures 1A and 1B). If a target was revisited within a trial, the monkey received a time-out and no reward. After each of the six targets was selected once, a new trial started after an inter-trial interval, signaled by a change in target color. Therefore, to perform well, the monkeys had to use WM to remember which targets had been visited and update this information after each selection.

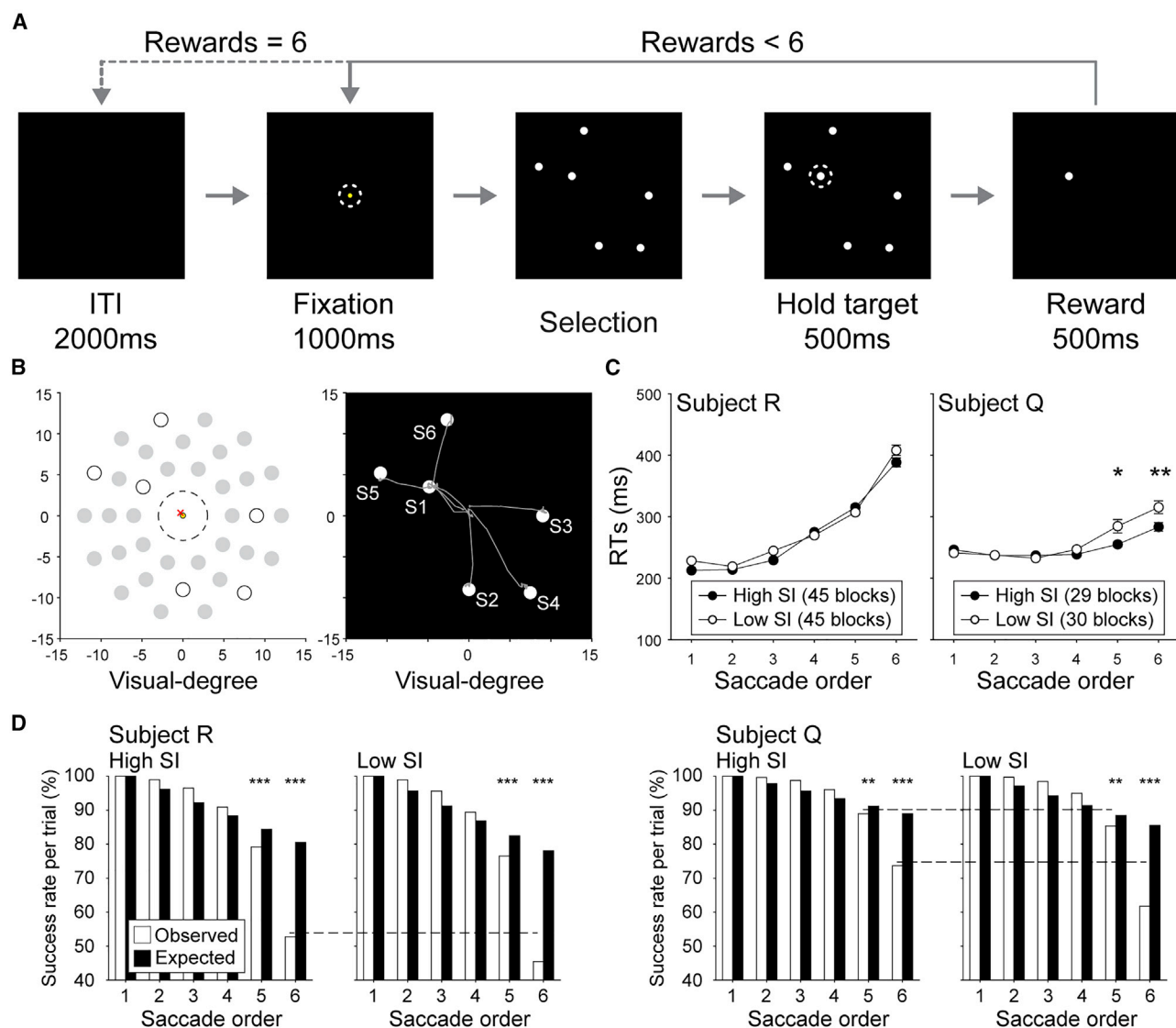
Each recording session consisted of six blocks of 40 trials, with target configurations held constant within a block. This allowed target selection patterns to be quantified within each

block. Previously, a measure of target sequencing, termed stereotyped index (SI), was defined to quantify the similarity of target selection patterns in a given block (see STAR Methods). Higher SIs indicated blocks in which targets tended to be visited in the same order, and lower SIs indicated blocks with more diversity in selection orders. Using this approach, SIs varied block to block, but there was no evidence for systematic changes in SI depending on the configuration of targets, the block number within a session, or the session number (Chiang and Wallis, 2018b) (Table S1). However, behavior patterns indicated that sequencing strategies improved WM performance. Revisit errors were not equally distributed across six target selections but occurred predominantly in the last two selections. This pattern suggests that monkeys used WM to complete the task (see STAR Methods), and the final targets exceeded a limited WM capacity (Chiang and Wallis, 2018b). Importantly, using a sequencing strategy improved both errors and reaction times (RTs) in these last two selections, suggesting that the strategy augmented WM performance (Figures 1C and 1D). In addition, it was shown that LPFC neurons encode the spatial and sequential information required to perform the target selection task (Chiang and Wallis, 2018b), but the amplitude of spatial tuning significantly decreased as target selection patterns became more stereotyped (Figure 2). This feature of stable spatial tuning with amplitudes modulated by task demands has previously been found in primate dIPFC in another self-organized behavioral task (Procyk and Goldman-Rakic, 2006).

### No loss of task information in LPFC ensembles with stereotyped behavior patterns

Populations of approximately 40 LPFC neurons were simultaneously recorded during task performance ( $47.27 \pm 2.72$  for subject R and  $36.80 \pm 2.14$  for subject Q; Table S1), allowing us to assess how task information is represented at the ensembles level. We created three decoders to examine representations of target locations (targets A–F), saccade orders (correct saccades 1–6, excluding revisits), and target colors (green, blue, and white). Each variable was decoded from ensembles of simultaneously recorded LPFC neurons using linear discriminant analysis (LDA) with leave-one-saccade-out cross validation (Figure S1; see STAR Methods). Classifier performance was assessed separately for each block of 40 trials. The feature matrices used for the three decoders were identical, with columns consisting of each recorded unit, and six correct saccade responses (revisit errors excluded)  $\times$  40 trials constituting the rows. The elements of the feature matrix were the mean firing rates in a given epoch.

We found that neural ensembles in LPFC represented both target locations and saccade orders (Figure 3B). These were decoded as categorical variables that changed across selections within a trial according to the onset time of the six-target configuration. In Figure 3B, the posterior probability of the selected target or current saccade number, but not target color, increased as the monkey initiated each saccade response. That is, when “target A” was selected, the posterior probabilities for A were high, and this pattern switched to B, then C, and so on, as each was subsequently selected (Figure 3B, top panel). Similarly, the posterior probabilities of the current saccade number



**Figure 1. Spatial self-ordered search task**

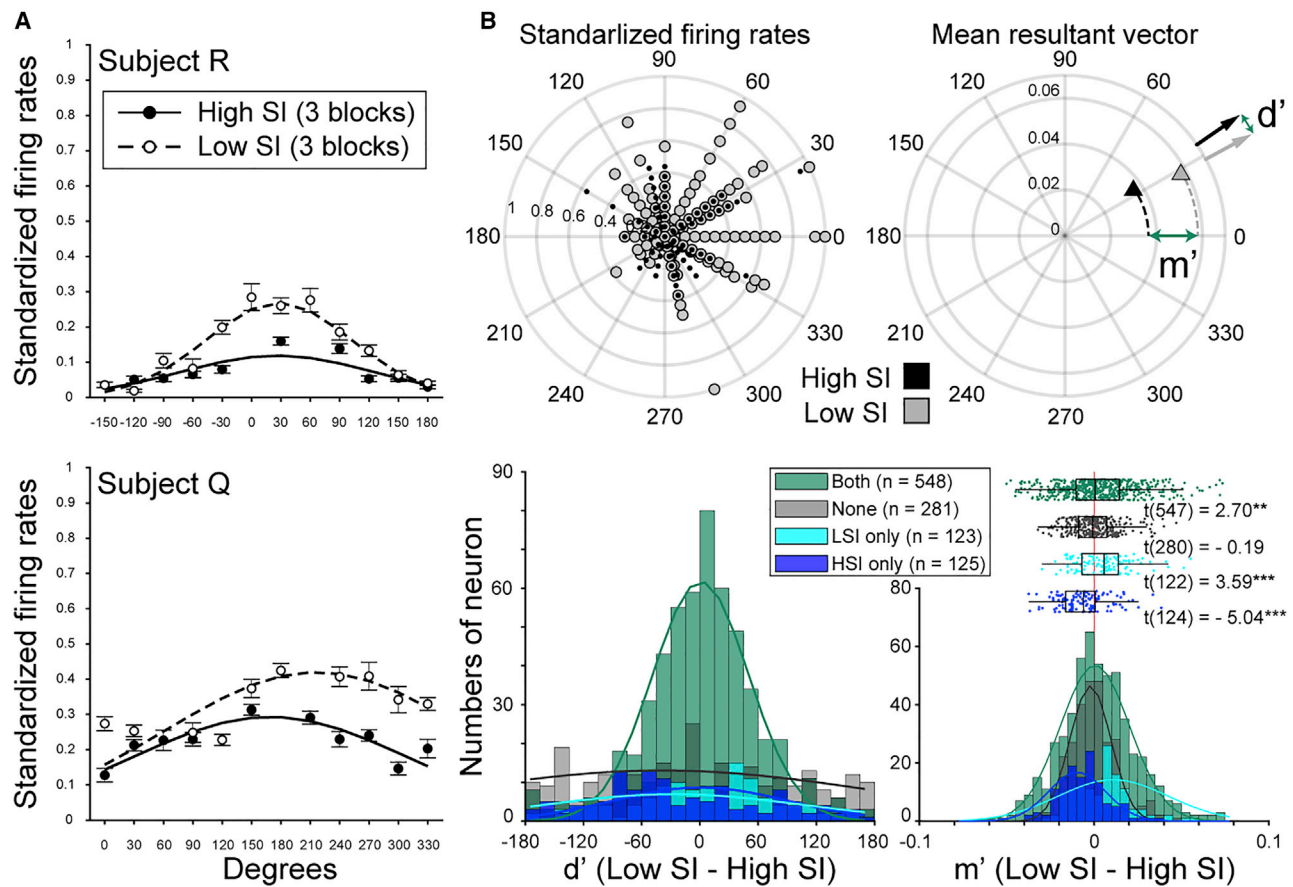
(A) On each trial, monkeys fixated a yellow point in the center of the screen and were shown a configuration of six identical targets (white circles). They made a selection (dashed line) by saccading to and holding fixation on one target. If the target had not been visited on that trial, a reward was delivered, and the monkey had to move its eyes back to the central fixation point before making another selection. This continued until all targets were visited once, at which point the trial ended and was followed by an inter-trial interval (ITI).

(B) An example trial with the target selection pattern. Gray trajectories indicate saccade paths starting from fixation to each target. S1–S6 indicates target selection order.

(C and D) Blocks were divided into high- and low-SI groups by a median split of each session. (C) A multiple linear regression model predicted RTs from saccade order, high- or low-SI block, and order  $\times$  block interaction. In both subjects, RTs increased across saccades, suggesting that later selections were more difficult (main effect of order,  $p < 0.001$  for both). For subject R, RTs during high-SI blocks were faster than during low-SI blocks (main effect of SI block,  $p < 0.05$ ), and for subject Q, there were faster RTs during high-SI blocks on the last two saccades (order  $\times$  SI block interaction,  $p < 0.001$ ; post hoc comparisons,  $^*p < 0.05$  and  $^{**}p < 0.01$ ). Error bars = SEM. (D) Monkeys make more errors than expected later in selection sequences. Expected success rates were calculated as a linear function of the number of potentially incorrect saccades possible at each selection (see [STAR Methods](#)), and observed rates were the number of correct selections divided by the total number of trials ([Chiang and Wallis, 2018b](#)). Monkeys performed better than the expected when WM loads were low, but performance declined precipitously when capacity was exceeded (binominal tests,  $^{**}p < 0.01$  and  $^{***}p < 0.001$ ). Performance was enhanced on high-SI blocks specifically during later target selections, when WM began to falter (chi-square tests, dashed lines indicate  $p \leq 0.01$ ).

also increased on each successive saccade (Figure 3B, middle panel). Overall, in a 500 ms time window after the monkey selected a target, the mean posterior probabilities ( $\pm$  SEM) for

the correct target location and saccade order were  $0.33 \pm 5 \times 10^{-3}$  and  $0.184 \pm 3.7 \times 10^{-3}$  for subject R and  $0.25 \pm 3.7 \times 10^{-3}$  and  $0.183 \pm 3.3 \times 10^{-3}$  for subject Q, respectively (for



**Figure 2. Sequencing strategies decrease spatial tuning among single neurons**

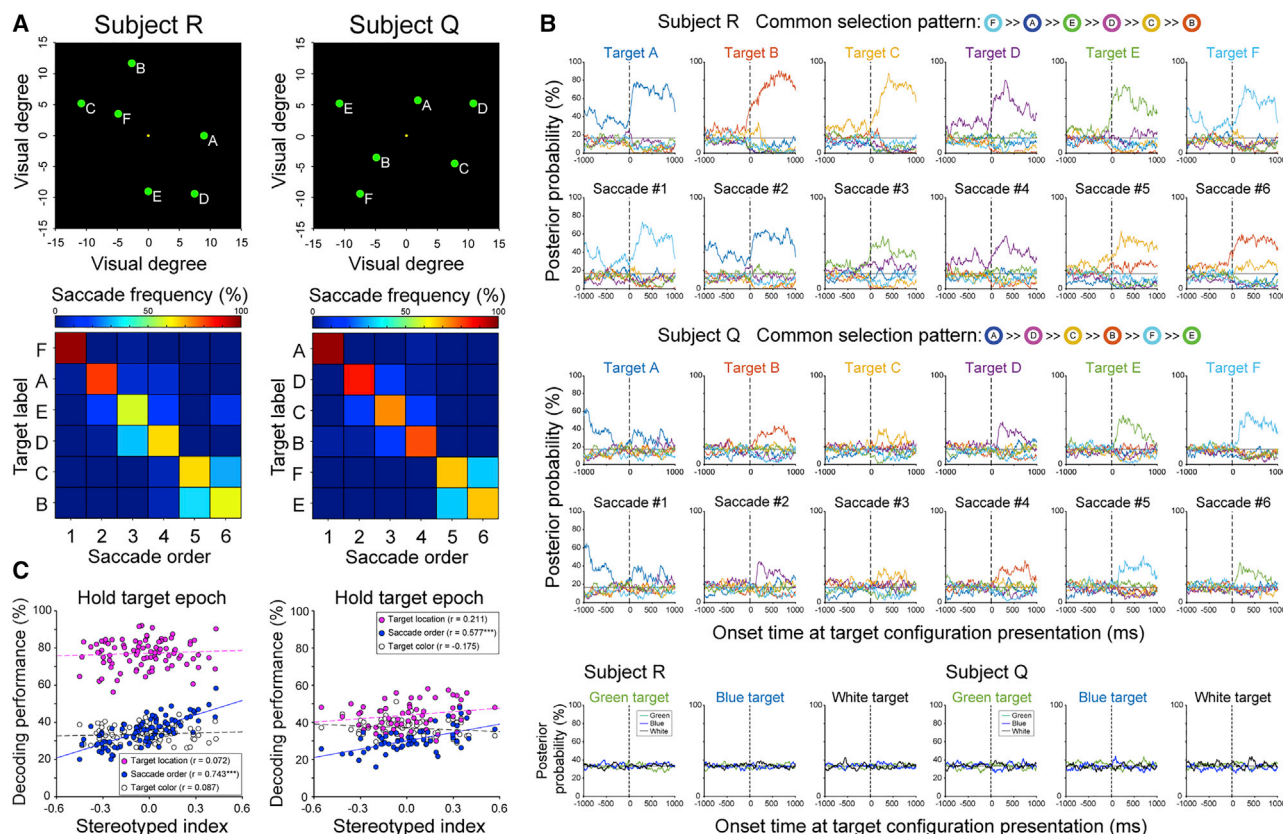
(A) Two single-neuron examples, recorded from subjects R (left) and Q (right), showing the effects of the sequencing strategies on spatial tuning. The x axis refers to the angle, in polar coordinates, of the selected target on the screen. Filled circles are from the three blocks in an exemplar session with higher SIs. Empty circles are from the three blocks in the same session with lower SIs. Error bars = SEM. Flatter tuning curves were observed when the animal was searching through the targets using a more stereotyped strategy (Chiang and Wallis, 2018b).

(B) Changes in spatial tuning were quantified by the change in direction ( $d'$ ) and magnitude ( $m'$ ) of resultant vectors for standardized firing rates in high- and low-SI blocks. The first circular plot shows standardized firing rates for one example neuron. The second shows the endpoints of the resultant vectors for each group (triangles), with  $m'$  and  $d'$  measures. Histograms show  $d'$  and  $m'$  for each single unit, grouped according to when they exhibited spatial selectivity: in both high- and low-SI blocks (green), low-SI only (cyan), high-SI only (blue), or neither (gray). The direction of spatial tuning shifted slightly in the high-SI group (blue; deviation from zero degrees,  $t_{124} = -2.51$ ,  $p = 0.013$ ), when directional tuning was weak. Other groups showed no shift in tuning direction ( $p > 0.05$ ). In contrast, there was consistently stronger tuning in low-SI blocks (positive  $m'$ ) among neurons that exhibited spatial tuning in low-SI only (cyan) or both low- and high-SI blocks (green), constituting the majority of recorded neurons. Those with spatial tuning in high-SI blocks only (blue) had significantly negative  $m'$  distributions, and those with no tuning (gray) had distributions centered at zero.  $^{**}p < 0.01$  and  $^{***}p < 0.001$ .

held-out data), significantly higher than those for the non-selected targets or incorrect saccade numbers ( $0.134 \pm 0.001$  and  $0.163 \pm 7.4 \times 10^{-4}$  for subject R and  $0.15 \pm 7.5 \times 10^{-4}$  and  $0.163 \pm 6.7 \times 10^{-4}$  for subject Q, respectively; Wilcoxon signed-rank test,  $p = 1.4 \times 10^{-86}$  and  $p = 0.01$  for subject R and  $p = 1.6 \times 10^{-58}$  and  $p = 3.0 \times 10^{-4}$  for subject Q). Therefore, both target location and saccade number could be decoded from LPFC ensembles. In contrast, posterior probabilities for target colors were close to chance level (Figure 3B, bottom panel) ( $0.333 \pm 1.1 \times 10^{-3}$  and  $0.334 \pm 5.7 \times 10^{-4}$  for subject R and  $0.348 \pm 1.8 \times 10^{-3}$  and  $0.326 \pm 8.9 \times 10^{-4}$  for subject Q, chance = 33.3%). This is likely because different colors were used only to indicate the beginning of a new trial and were not themselves relevant to performance of the WM task.

Next, we examined how stereotyped selection patterns interact with our ability to decode the three task variables during the epoch of highest decoder performance (hold target epoch, 500 ms following each saccade; Figure S2). On the basis of the earlier finding that single neurons were less spatially tuned when behavior was more stereotyped, we anticipated poorer decoding of target locations in higher SI blocks. However, this was not the case. Figure 3C shows that decoding performance for each variable was unaffected or improved in higher SI blocks. To quantify this, we performed a two-way analysis of covariance (ANCOVA) on decoding performance with continuous variable SI and categorical variable decoder type. There were significant main effects of decoder type ( $F_{[2, 264]} = 1,670.55$ ,  $p < 0.001$ , for subject R;  $F_{[2, 171]} = 87.96$ ,  $p < 0.001$ , for subject Q) and SI





**Figure 3. Target location and saccade order, but not target color, can be decoded from LPFC ensembles**

(A) Two sample target configurations with saccade frequency matrices from two subjects. Targets at unique locations were arbitrarily assigned letters for analysis. The matrices show the proportion of trials within a block that each target was selected first, second, and so on. These example blocks show strong sequencing behavior, with high frequencies on the main diagonal.

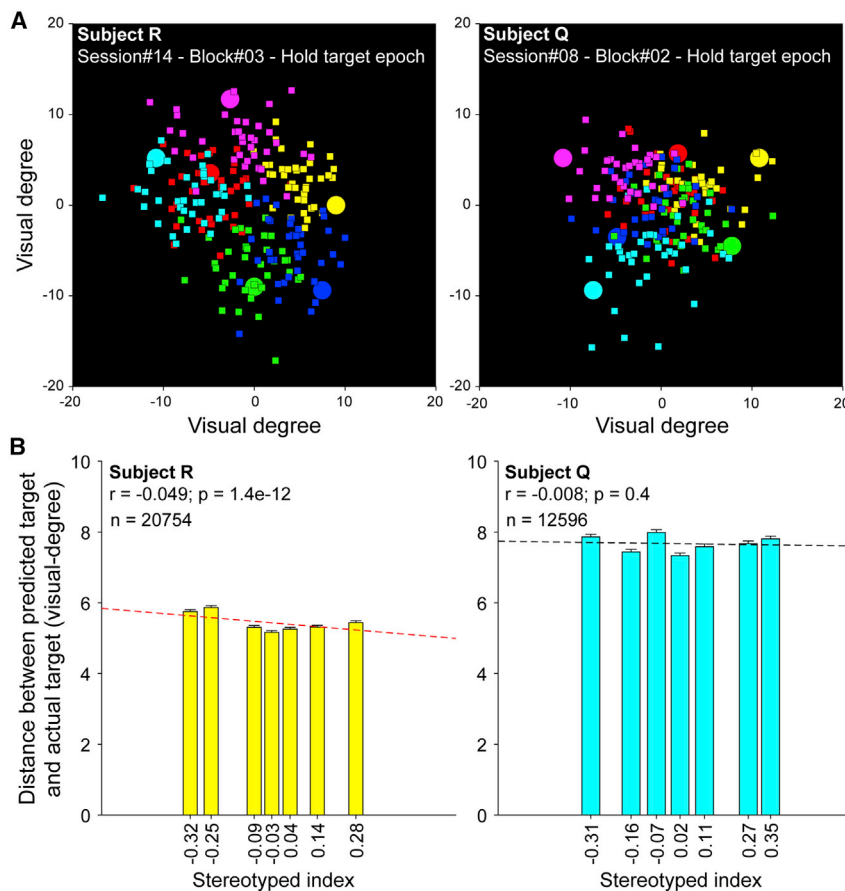
(B) Posterior probabilities calculated for each of six target selections, across 40 trials from the same blocks shown in (A). The top and middle panels show posterior probabilities of target locations and saccade orders from both subjects, and the bottom panel shows target color. Dotted lines indicate the onset time of the target configurations, and gray lines indicate the chance level. The common saccade order was defined by the sorted saccade frequencies in (A). Color labels indicate different targets or target colors.

(C) The decoding performance during the hold target epoch for target location (pink circles), saccade order (blue circles), and target color (empty circles) decoders, as a function of SI in each block. Pearson correlation, \*\*\*p < 0.001. Left panel: subject R (n = 90 blocks); right panel: subject Q (n = 59 blocks).

( $F_{[1, 264]} = 36.61$ ,  $p < 0.001$ , for subject R;  $F_{[1, 171]} = 11.07$ ,  $p = 0.0011$ , for subject Q), with better decoding of target locations compared with the saccade orders and target colors in both monkeys. In addition, there were significant interactions between SI and decoder type in both subjects ( $F_{[2, 264]} = 22.59$ ,  $p < 0.001$ , for subject R;  $F_{[2, 171]} = 8.76$ ,  $p < 0.001$ , for subject Q), with performance of the saccade order decoder improving with higher SI but target location and color decoders remaining unchanged. This was confirmed by post hoc comparisons showing that target location decoding did not depend on SI in either subject (Pearson correlation,  $r = 0.07$ ,  $p = 0.502$ , for subject R;  $r = 0.21$ ,  $p = 0.108$ , for subject Q), but saccade order decoding improved with higher SI (Pearson correlation,  $r = 0.74$ ,  $p < 0.001$ , for subject R;  $r = 0.58$ ,  $p < 0.001$ , for subject Q). More sequenced behaviors did not appear to activate multiple target representations simultaneously. When blocks were pooled into high-SI (HSI) and low-SI (LSI) groups by a median split of behavior in each session, there was consistently better decoding

of the current target location or saccade position on HSI blocks but no changes in information about the immediately preceding or following selections (Figure S3). Finally, there were no correlations between performance of target color decoder and SI (Pearson correlation:  $r = 0.08$ ,  $p = 0.414$ , for subject R;  $r = -0.18$ ,  $p = 0.184$ , for subject Q). Together, results from both subjects showed equal or better decoding of task variables as behavior became more stereotyped, despite loss of spatial tuning among single neurons.

Given these results, one possibility is that as SI increases, target identities and saccade orders become more correlated, so that a decoder for either variable could improve by relying on information about both categories rather than just one. Despite this correlation, however, the performance of the two task-relevant decoders did not converge at higher SIs, suggesting that the representations were not completely overlapping (Figure 3C). Further analyses using partial correlations revealed that better saccade order decoding at higher SIs was accounted



**Figure 4. Two-dimensional spatial decoding**

(A) Example target configurations, in which each target (circles) is color coded, to show the corresponding predicted target locations (squares). Different color labels were used for visualization only; targets in the task were identical. Note that the decoder was trained and tested across blocks with different SIs and target configurations but the same neuron ensemble.

(B) Decoding performance was quantified for each target selection as the Euclidean distance between actual and predicted targets, and plotted as a function of SI. Performance improved with SI in subject R and was unaffected in subject Q, demonstrating no loss of spatial information at the population level with more stereotyped behaviors. For data visualization, the original scatterplots (Figure S5) were binned by SI into seven subgroups with an equal number of observations in each. The SI value on the x axis for each bar is the mean of SIs within the subgroup. Error bars = SEM.

for largely by correlations with target location, but the accuracy of target location decoding increased with higher SIs after controlling for the actual X,Y position and saccade order (Figure S4A; Table S3). We also examined each unit's mean firing rate as the independent variable rather than decoder performance and found no tendencies toward weaker or stronger relationships between firing rate and saccade order or target identity as SI increased (Figure S4B), meaning that changes in mean firing rate do not explain how decoder performance was maintained during more stereotyped performance.

Shared variability among neurons has been shown to affect information decoding, either positively or negatively (Ben Hadj Hassen and Ben Hamed, 2020; Cohen and Kohn, 2011; Nogueira et al., 2020; Tremblay et al., 2015), so we tested whether there were systematic changes in noise correlations in blocks in which monkeys' behavior was more stereotyped. We assessed whether the proportion of neuron pairs with correlated variability changed across blocks with different SIs but did not find reliable evidence for consistent effects (Table S4). Therefore, it is unlikely that decoding accuracy was affected by systematic changes in noise correlations across blocks.

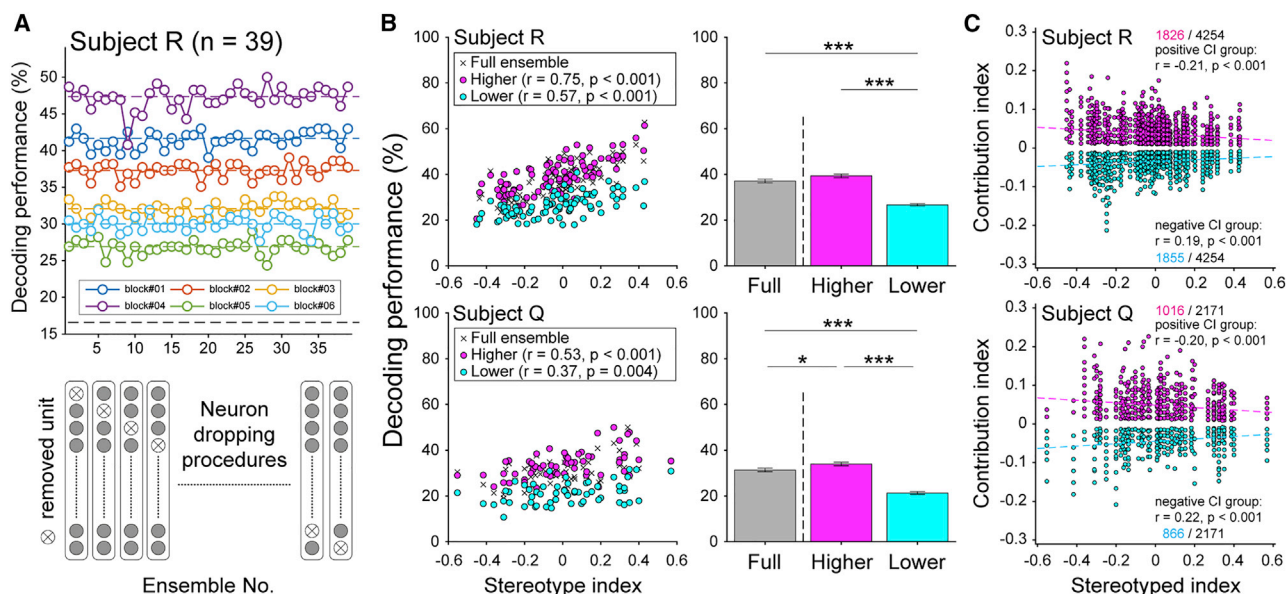
Finally, because LDA classifiers may have been subject to ceiling effects in target decodability (Figure 3C), we assessed a more sensitive measure of spatial information in LPFC ensembles that

is independent of saccade order. We decoded two-dimensional (2D) spatial coordinates for each target from the same neural activity feature matrix including all trials in a recording session (i.e., across blocks with different SIs) (Astrand et al., 2016). To define decoding performance, we found the Euclidean distance between predicted and actual target locations. A small distance indicated a prediction that was close to the selected target and therefore accurately decoded.

We found that performance of the 2D spatial decoder improved as SI increased in subject R, and there was no change with SI in subject Q (Pearson correlation:  $r = -0.049$ ,  $p < 0.001$ , for subject R;  $r = -0.008$ ,  $p = 0.399$ , for subject Q) (Figure 4). Therefore, despite reductions in spatial tuning at the single-neuron level, there was again no loss of accuracy in decoding target locations from ensembles of the same neurons.

#### Single units make different contributions to ensemble codes

To understand how population coding changed when monkeys used sequencing strategies, we assessed the contributions of each unit to the ensemble's decoding performance using a neuron dropping procedure (Narayanan et al., 2005; Nicolelis, 1998). First, we found the accuracies of LDA classifiers trained and tested on  $n - 1$  ensembles, in which one unit was iteratively removed from a full ensemble of size  $n$ . A unit's unique contribution was quantified by the difference in performance between the full and  $n - 1$  ensembles, with reductions in decoding accuracy corresponding to positive contributions and improvements in decoding accuracy corresponding to negative contributions. This approach takes interactions between neurons into account, as neurons providing redundant information would have approximately zero contribution.



**Figure 5. Units make smaller contributions to the ensemble when behavior is more sequenced**

(A) Diagram of the neuron dropping procedure in a sample recording session. Six blocks from the same session are labeled by different colors. Average performance from a saccade order decoder (y axis) varied across blocks. In the neuron dropping procedure, the same decoder was run while iteratively removing one unit from the ensemble (bottom schematic).

(B) Scatterplots show block-wise mean saccade order decoding as a function of SI for the full ensemble (+), higher contribution (magenta), and lower contribution (cyan) subgroups. Decoding performance corresponds to the proportion of target selections accurately classified. Bar plots show the overall means, collapsed across SI (pairwise t tests,  $*p < 0.05$  and  $***p < 0.001$ ). Error bars = SEM.

(C) Population data showing CI as a function of SI. Each point is the contribution of one neuron to one block. Neurons making positive contributions (magenta) improved decoder performance, while those making negative contributions (cyan) reduced it. The contributions of the positive groups decreased as SI increased, and contributions of the negative groups increased as SI increased.

Six exemplar blocks in the top panel of Figure 5A show decoding of saccade order using  $n - 1$  ensembles, where the horizontal line is the median performance in that block, and each circle is performance with a different held-out neuron. These blocks were recorded from the same session, so the ensemble remained constant, illustrating how the contributions of the same neuron can vary across blocks with different target configurations. In the full dataset, only rare neurons (16 of 1,077 [1.5%]) kept the same type of informative contribution consistently across blocks. In addition, there were differences in median decoding performance across blocks within a recording session, implying that decoding depends on the target configurations and/or block-wise changes in behavior.

To determine whether some neurons consistently contribute more to population decoding, we separated each full ensemble into two sub-ensembles. If a given neuron's contribution was greater than or equal to the median decoding performance in at least three of six blocks in a session, that neuron was included in the higher contribution subgroup, and the remainder were included in the lower contribution subgroup. Consistent with our earlier results, we found that decoding improved in blocks in which selection patterns were more sequenced, and the higher contribution subgroup performed similarly to the full ensemble (Figure 5B). In addition, decoding performance was lower among the low-contribution group but still tended to increase with SI (SI  $\times$  contribution group ANCOVA; main effect

of SI:  $F_{[1, 176]} = 151.86$ ,  $p < 0.001$ , for subject R;  $F_{[1, 114]} = 30.4$ ,  $p < 0.001$ , for subject Q; main effects of contribution groups:  $F_{[1, 176]} = 343.6$ ,  $p < 0.001$  for subject R;  $F_{[1, 114]} = 205.43$ ,  $p < 0.001$ , for subject Q; interaction:  $F_{[1, 176]} = 17.02$ ,  $p < 0.001$ , for subject R;  $F_{[1, 114]} = 2.61$ ,  $p = 0.109$ , for subject Q). In post hoc comparisons, both contribution groups were positively correlated to the SI (Pearson correlations; higher contributions:  $r = 0.75$  and  $r = 0.53$ ,  $p < 0.001$  for both, for subjects R and Q; lower contributions:  $r = 0.57$  and  $r = 0.37$ ,  $p < 0.001$  and  $p = 0.004$ , for subjects R and Q). In comparison with the full ensemble, the higher contribution groups achieved similar or higher accuracies, while the lower contribution group performed worse (mean  $\pm$  SEM:  $0.39 \pm 0.008$  full,  $0.37 \pm 0.008$  high, and  $0.27 \pm 0.005$  low for subject R;  $0.31 \pm 0.008$  full,  $0.34 \pm 0.008$  high, and  $0.21 \pm 0.006$  low for subject Q). One-way ANOVA on decoding performance with post hoc comparisons confirmed these results ( $F_{[2, 269]} = 85.83$ ,  $p < 0.001$ , for subject R;  $F_{[2, 176]} = 81.63$ ,  $p < 0.001$ , for subject Q; Bonferroni-corrected post hoc comparisons: full versus high:  $p = 0.078$  and  $p = 0.034$ ; full versus low:  $p < 0.001$  for both; high versus low:  $p < 0.001$  for both, subjects R and Q). Thus, the neural representations of saccade orders could be extracted from subsets of the full recorded population, and removing the less informative neurons had little effect on accuracy. We found similar results from the target location decoder (Figure S6). This emphasizes that there is variability and potentially redundancy in the contributions



individual neurons make to population codes (Hung et al., 2005; Meyers et al., 2008; Narayanan et al., 2005)

Next, we wanted to determine whether the contributions of neurons changed as the monkeys' target selection patterns became more sequenced. To better understand this question, we created a standardized contribution index (CI) for each unit in each block, defined as the ratio of the difference between the mean decoding performance from the full ensemble ( $n$ ) and the  $n - i$  ensemble after removing neuron  $i$  (see STAR Methods). Positive or negative CIs indicate that neuron  $i$  improved or reduced the decodability, respectively, and zero CI indicates that the neuron provided redundant information or made no contribution to decoding. Using this approach, we found that the proportion of positive or negative CI units did not vary with SI (Pearson correlations,  $p > 0.05$  for all), but the magnitudes of both positive and negative CIs decreased as behavior became more stereotyped (Figure 5C). In the target location decoder, this effect was stronger for positive compared with negative CIs (Figure S6). This was confirmed by significant interactions in two-way ANCOVAs (SI  $\times$  contribution type) predicting CI in both monkeys ( $F_{[1, 3,677]} = 148.67$ ,  $p < 0.001$ , for subject R;  $F_{[1, 1,878]} = 85.56$ ,  $p < 0.001$ , for subject Q). Post hoc comparisons revealed that for the saccade decoder, neurons with positive contributions were negatively correlated with SI, while those with negative contributions were positively correlated ( $n = 1,826$  and  $n = 1,016$  positive,  $n = 1,855$  and  $n = 886$  negative out of  $n = 4,254$  and  $n = 2,171$  neuron-blocks for subjects R and Q, respectively; Pearson correlations: positive:  $r = -0.21$  and  $r = -0.20$ ,  $p < 0.001$  for both, for subjects R and Q; negative:  $r = 0.19$  and  $r = 0.22$ ,  $p < 0.001$  for both, for subjects R and Q), and similar results were found for the target location decoder (Figure S6). Therefore, the contributions of single neurons to an ensemble's decoding performance consistently decreased in magnitude as behavior became more stereotyped. This suggests fundamental changes in the population codes for task-relevant information in LPFC under different self-generated cognitive strategies. In addition, the diversity of contributions among both positively and negatively contributing neurons became smaller during routine behavioral strategies. This is consistent with smaller, more homogeneous contributions to decoding performance and may reflect loss of strong tuning among single neurons, as previously described (Chiang and Wallis, 2018b). Together, these analyses show that units make unequal contributions to the overall representation, and these contributions can change under varying behavioral patterns. With this in mind, we next address the question of why task-relevant decoders perform as well or better when individual neurons make smaller contributions under more stereotyped behavioral strategies.

### Optimal ensemble sizes varied by behavioral strategy

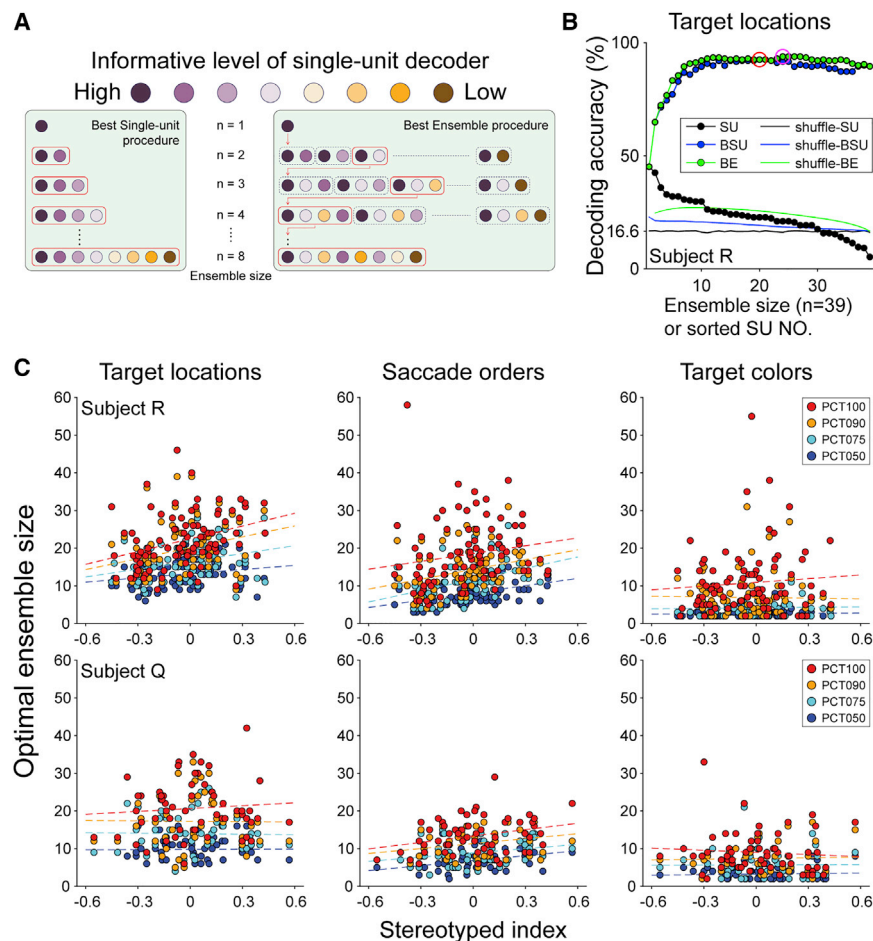
Our findings so far show that, when decoding task information, some neurons in an ensemble are redundant or non-contributing. This means that in a recorded population, the best decoding accuracies can be achieved with less than the full ensemble. To better understand ensemble coding and how it changes, we determined the optimal ensemble size for maximum decoding in each trial block. We used two approaches, best single-unit (BSU) and best ensemble (BE) procedures, to assess how decoding performance changes as ensemble size gradually increases

(Backen et al., 2018; Leavitt et al., 2017). Both BSU and BE add units one at a time into the ensemble to build feature decoders (Figure 6A) but differ in how they select which neuron to add. The BSU procedure rank-orders the decoding performance of all single-unit (SU) decoders and then adds units one at a time by descending rank into the ensembles. In contrast, the BE procedure takes all possible combinations of units into account and increases the ensemble size by adding whichever unit leads to the maximum decoding performance. Both procedures are performed iteratively until all units have been added.

Following both BSU and BE procedures, we decoded three variables for each block: target location, saccade order, and target color. Decoding was conducted with LDA, and accuracies were based on leave-one-out cross validation. Decoding accuracies improved and eventually became asymptotic as ensemble sizes increased under either the BSU or BE procedure (Figure 6B; Figure S7). Optimal ensemble sizes were defined as the smallest size to achieve maximum (100th percentile [PCT100]) decoding performance. Because accuracy curves fluctuated slightly around the plateau, we also identified the ensemble sizes corresponding to the 50th percentile (PCT50), 75th percentile (PCT75), and 90th percentile (PCT90) of the maximum decoding performance in each block for further analyses. Compared with BSU, BE produced higher maximum performance in all three types of decoders because it takes into account how redundant or complementary the units in the ensemble are. The color decoders performed closest to shuffled baselines, indicating that color information is weakly represented compared with the target locations or saccade orders (Figure S7A). Optimal ensemble sizes for target location and saccade order tended to be positively correlated (Figure S7B), so that blocks in which more neurons were required to reach maximum accuracy in spatial decoding also required more neurons to accurately decode saccade order. Interestingly, these co-varying ensemble sizes also appeared to correlate with SI, such that lower SI blocks tended to have smaller optimal ensemble sizes. To quantify this observation, we performed two-way ANCOVAs with categorical factor PCT and continuous factor SI predicting optimal ensemble size and found that ensemble sizes increased with SI for the saccade decoder in both animals (Figure 6C) (significant main effect of SI:  $F_{[1, 228]} = 32.77$ ,  $p < 0.001$ , for subject R;  $F_{[1, 228]} = 20.98$ ,  $p < 0.001$ , for subject Q) and for the target decoder in one animal ( $F_{[1, 352]} = 33.70$ ,  $p < 0.001$ , for subject R;  $F_{[1, 228]} = 0.10$ ,  $p < 0.76$ , for subject Q). In contrast, decoding of color, which was less relevant to the working memory component of the task, did not vary with SI in either animal ( $F_{[1, 352]} = 0.41$ ,  $p = 0.52$ , for subject R;  $F_{[1, 228]} = 0.02$ ,  $p = 0.88$ , for subject Q). Overall, these data demonstrate that optimal ensemble sizes for decoding task-relevant, but not irrelevant, information increased as the SI increased, so that more neurons were required to accurately decode task-relevant information when behavioral strategies became more stereotyped.

### Neural dimensionality varies by behavioral strategy

According to the results above, strategy use in the self-ordered WM task decreased single-neuron contributions to ensemble coding and increased optimal ensemble sizes for task-related



**Figure 6. Optimal ensemble sizes increase with SI**

(A) Schematic of BSU and BE procedures adapted from Backen et al. (2018) and Leavitt et al. (2017). In the BSU procedure, the information carried by each neuron is determined by a single-unit decoder, and the ensemble size is gradually increased by iteratively adding units on the basis of their information rank. The BE procedure starts with the most informative neuron, then tests all possible combinations of neurons to iteratively select one that produces the maximum decoding performance at that step.

(B) Performance of the target location decoder from subject R in an example block. Black symbols show ordered single-unit decoders. Filled circles show BSU (blue) and BE (green) accuracies as neurons are added to the ensemble. Red and magenta circles indicated the ensemble size with maximum decoding accuracies for each approach. The same procedures were also used on shuffled datasets (BSU in blue, BE in green, and single unit in black lines; see STAR Methods). Note that BSU and BE procedures selected ensembles optimized to decode real or shuffled data, so that shuffled accuracies are slightly above theoretical chance, as observed in other studies (Backen et al., 2018; Leavitt et al., 2017). The chance level for target location and saccade order decoders was 16.6% and for target color decoder was 33.3%.

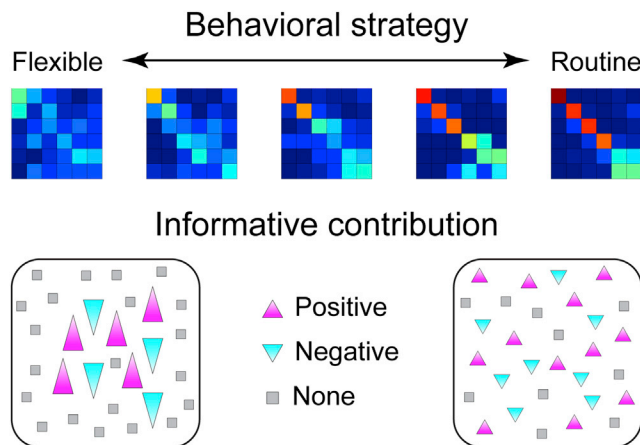
(C) Optimal ensemble sizes increase with sequencing. Optimal ensemble sizes at each PCT as a function of SI for target location, saccade order, and target color decoders from two subjects. Ensemble sizes were higher with high SI for task-relevant (location and order) but not irrelevant (color) information.

decoding. In a final analysis, we focused on whether these changes are reflected in the dimensionality of LPFC activity under different behavioral strategies. We specifically investigated dimensionality over the time course of the six correct saccades in each trial and determined how it varied with SI across successive saccades.

Our previous results showed that reaction times increased and success rates decreased across saccades (Chiang and Wallis, 2018b), suggesting that WM loads increased as the monkey progressed through six target selections and kept track of which had already been selected. Thus, dimensionality of neural responses may be affected by WM load as well sequencing strategies that impose structure on that information held in mind. Different measures of dimensionality in neural populations have been used in different experimental systems (Abbott et al., 2011; Ganguli and Sompolinsky, 2012; Gao and Ganguli, 2015; Rigotti et al., 2013). Here, we used the participation ratio (PR), which finds the number of dimensions needed to explain about 80%–90% of the total variance in a population covariance matrix (Dąbrowska et al., 2021; Gao et al., 2017). We computed the covariance matrices from average firing rates in 20 ms non-overlapping bins that spanned four trial epochs around each correct saccade (Figure S1). Therefore, the resulting PR reflects

similarities in the pattern of firing rates across neurons on each saccade, and a low PR can be interpreted as a more homogeneous firing rate profile.

To determine how PR varied across saccades, we created a multiple linear regression model to predict PR from saccade number (1–6) and SI in the corresponding block for each monkey. Only correct saccades were included, and PRs within each session were Z scored to make different recording sessions comparable. In addition, a third predictor indicated the number of simultaneously recorded signals in the corresponding recording session, as this can affect PR values (Mazzucato et al., 2016). Overall, this model significantly explained dimensionality changes across target selections in both subjects ( $p < 0.001$  for subjects R and Q). The PR was positively correlated with saccade number ( $b_1 = 0.027$  and  $b_1 = 0.019$ ,  $p < 0.001$  for both, for subjects R and Q) and negatively correlated with SI ( $b_2 = -0.081$  and  $b_2 = -0.088$ ,  $p < 0.001$  for both, for subjects R and Q). Therefore, as the WM load increased across saccades, patterns of firing rates become more diverse (i.e., more eigenvectors were needed to capture the same amount of variance). Note that this result does not imply that saccade order is encoded as dimensionality but rather that the diversity of firing rate patterns increases as the monkey proceeds through six



**Figure 7. Sequencing strategies shift information from single units to populations**

Top: self-generated strategies varied across blocks, from flexible to routine. Selection frequencies for example blocks are similar to Figure 2, with warm colors on the diagonal indicating that selections frequently occur in the same order. Bottom: schematic of neural ensembles from the extremes of the flexible-routine spectrum. Triangle size indicates the amplitude of each neuron's contribution. When strategies are more routine, larger groups of units with smaller individual contributions are recruited; otherwise, task information is represented by smaller groups of units with larger individual contributions.

target selections in a trial. On the other hand, when monkeys enlist sequencing strategies, this diversity is reduced, consistent with the notion that these strategies reduce WM load. Together, these dynamic changes of dimensionality suggest that firing patterns in neural ensembles become more diverse when more information is needed for successful performance (e.g., remembering selected targets) and return to their initial status when a new trial begins and the information held in WM resets. In addition, dimensionality was modulated by a cognitive strategy that improved WM performance. Therefore, neural dimensionality reflects not only behavior-related states such as motor preparation (Churchland et al., 2006) and resting state (Dąbrowska et al., 2021) but also task demands such as rule learning (Bartolo et al., 2020; Durstewitz et al., 2010), cognitive strategies, and WM loads.

## DISCUSSION

When a cognitive task exceeds the limits of our WM abilities, performance can be improved with mnemonic strategies that organize the information held in mind. One common strategy is to remember lists that arrange items in an arbitrary sequence (Desrochers et al., 2010, 2015; Ericsson and Kintsch, 1995; Lashley, 1951). This process likely relies on the LPFC, an area that plays a role in both WM and the use of mnemonic strategies. Supporting this, previous studies have shown that LPFC neurons demarcate boundaries of well-learned sequences (Fujii and Graybiel, 2003), and blood-oxygen-level-dependent (BOLD) signals in human LPFC increased when structured sequences were recognized (Bor et al., 2003). However, little is known about how an organizing structure such as a sequence changes coding of mnemonic information. In this study, we found that self-generated

sequencing strategies reorganize ensemble-level coding of task information in LPFC, such that more stereotyped behaviors were governed by more distributed codes. Distributed coding that relies less on strongly tuned neurons may be more robust and generalizable (Morcos et al., 2018), and our results suggest that distributed codes are also used to optimize performance of capacity-limited WM networks.

To summarize empirical findings from behavior, single units, and ensembles in this task, we propose a schematic of how representations change with the implementation of sequencing strategies (Figure 7). Behaviorally, monkeys appear to use WM to perform the task, making fewer errors on early saccades, when visited targets can be held in mind, but many more errors on the last saccades, when the list of visited targets exceeded WM capacity. To solve this task, subjects were able to generate flexible or routine (i.e., sequenced) target selection patterns, and the latter improved behavioral performance, measured as fewer target revisits per trial. This benefit occurred primarily on the final saccades, when WM begins to falter, indicating that sequencing behavior allowed the monkeys to overcome capacity limits on WM. We found that task-relevant information, including target locations and saccade orders, could be decoded from LPFC neural ensembles, and decoding accuracy tended to improve when monkeys' selection patterns were more stereotyped. However, this improvement was not intuitively explained by previous work showing that in the same neurons, the amplitude of spatial tuning decreased when the monkeys used more routine strategies (Chiang and Wallis, 2018b). To reconcile these seemingly contradictory results, we showed that individual neurons made smaller contributions to ensemble decoding when the monkey's behavior was more sequenced, while at the same time the ensemble sizes that optimized decoding performance increased. These results explain how decoding accuracy was maintained despite reduced spatial tuning among individual neurons. As the monkeys followed a more routine sequence, task information at the population level consisted of smaller contributions from a greater number of units. Consistent with this, we found that dimensionality of firing rates decreased when more routine strategies were adopted, meaning that the activity patterns became more homogeneous across the population. Overall, we conclude that representations of task information become more distributed in LPFC ensembles when monkeys use a sequencing strategy. These distributed representations may overcome WM constraints, perhaps by increasing the fidelity of information critical for task performance.

Our results emphasize how single units and populations provide different views of neural coding (Stokes et al., 2013). It is generally, if tacitly, assumed that information encoded by an ensemble must be present in the tuning properties of the component neurons when they are examined in isolation. However, there is accumulating evidence that classic tuning curves do not convey a full picture of the information present at an ensemble level (Pouget et al., 1999; Zhang and Sejnowski, 1999). For instance, ensemble codes for WM are affected by correlated variability among constituent neurons, with optimal coding commonly relying on units that are poorly tuned in a classical sense (Leavitt et al., 2017). Similar population interactions also change ensemble representations of visual space,

independent of individual neuron tuning (Dehaqani et al., 2018). In simulations, the presence of non-classical value-related responses in a population improves value decoding (Enel et al., 2021), and at the level of fMRI, adding non-selective voxels that appear irrelevant to stimulus coding nonetheless improves the performance of a stimulus decoder (Yamashita et al., 2008). Thus, the stimulus-related tuning of individual units does not necessarily dictate their importance to population-level codes.

Beyond simply representing information, distributed codes may play other important roles in network functions. For instance, artificial neural networks have suggested that distributed codes are more robust and generalizable. Compared with networks that used rote memorization to recognize images, those that learned generalizable concepts relied less on units that were selective for individual features (Morcos et al., 2018). The networks that developed fewer classically tuned units not only generalized better to new images but were also more robust to noise or unit ablation. Therefore, the selectivity of individual units is often a poor predictor of network performance, and this is echoed in our finding that monkeys tended to perform better in blocks in which single units exhibited less spatial tuning.

An open question is what benefit less tuned, more distributed representations might confer compared with other possibilities, such as populations that maintain single-unit selectivity but distribute the information among more tuned neurons. One consideration is that the latter coding scheme may be metabolically costly. Theoretical work has emphasized that neural codes likely evolved to optimize the trade-off between representational capacity and energy expenditure (Levy and Baxter, 1996). As metabolic costs per bit of information increase with bit rate (Laughlin et al., 1998), distributing information across populations should favor lower activity among individual neurons, which might manifest as reduced tuning. Another possibility is that reduced tuning could arise if neurons increasingly multiplex information as behavior becomes more routine. Neurons with mixed selectivity appear less classically tuned for single variables (Rigotti et al., 2013), and such mixing of task variables increases with task training in LPFC neurons (Dang et al., 2021). In our data, we found no evidence that past or future targets or saccades are increasingly represented with routine behavior, but it remains possible that other contextual or environmental information could mix with target information as selection order becomes more fixed, making neurons appear less tuned. Indeed, the context dependence of habitual behaviors (Thraillkill and Bouton, 2015) suggests that task and environmental information could become linked with repetition.

We found that distributed neural codes not only correlated with improved behavioral performance but were also implemented on the fly, as the monkey generated different strategies in a challenging task. This emphasizes the adaptability of prefrontal neurons under different conditions and goals. Although distributed coding led to better behavioral performance, different patterns of behavior, and their concomitant neural codes, are desirable under different conditions. Flexibility and exploration are frequently important, so we would not want to organize all behavior into structured sequences. If distributed coding is

part and parcel of more stereotyped behavior, it may be observed more commonly when behaviors become routine or overtrained, or when facing familiar situations. Indeed, as monkeys were trained on multi-item WM or association tasks over several weeks, more LPFC neurons became selective, but with lower average firing rates, suggestive of a more distributed code (Asaad et al., 1998; Tang et al., 2019). Different mnemonic strategies may also be used to overcome WM constraints. We commonly group a series of items into “chunks” or subgroups (Chiang and Wallis, 2018a), for instance when remembering telephone or Social Security numbers, and it remains to be seen whether these strategies also depend on distributed neural codes. Beyond behavioral circumstances that might promote more flexible or strategic behaviors, the underlying neuronal responses themselves may be constrained by metabolic costs, as discussed above (Levy and Baxter, 1996). For instance, increased BOLD signals have been found in human LPFC when subjects performed sequenced responses that lowered WM loads (Bor et al., 2003), suggesting that imposing structure on mnemonic representations entails an energetic cost. Thus, a balance of biological and behavioral benefits may ultimately influence how LPFC codes WM information.

In summary, implementing a cognitive strategy in a self-ordered WM task improved performance and shifted information from highly tuned single units to distributed ensemble representations. These results provide a novel view of how WM information is internally manipulated, without changes in external stimuli or task requirements. The mechanisms that dictate when and how information is distributed among a population remain to be investigated further, but could involve online adjustments in synaptic weights, as proposed under the “activity-silent” model of WM (Stokes, 2015). The present results provide the first step toward such investigations and reveal important insights into the mechanisms underlying advanced cognitive abilities such as implementing mnemonic strategies.

## STAR★METHODS

Detailed methods are provided in the online version of this paper and include the following:

- KEY RESOURCES TABLE
- RESOURCE AVAILABILITY
  - Lead contact
  - Materials availability
  - Data and code availability
- EXPERIMENTAL MODEL AND SUBJECT DETAILS
- METHOD DETAILS
  - Spatial self-ordered search task
  - Neurophysiological procedures
- QUANTIFICATION AND STATISTICAL ANALYSIS
  - Spatial tuning
  - Categorical decoders
  - Two-dimensional spatial decoder
  - Noise correlations
  - Neuron dropping procedure
  - Optimal ensemble size measures
  - Dimensionality measurement



## SUPPLEMENTAL INFORMATION

Supplemental information can be found online at <https://doi.org/10.1016/j.neuron.2021.11.021>.

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## AUTHOR CONTRIBUTIONS

F.-K.C. and J.D.W. designed research. F.-K.C. performed research. F.-K.C. and E.L.R. analyzed data. F.-K.C., J.D.W., and E.L.R. wrote the paper.

## DECLARATION OF INTERESTS

The authors declare no competing interests.

## INCLUSION AND DIVERSITY

One or more of the authors of this paper self-identifies as a member of the LGBTQ+ community.

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## STAR★METHODS

## KEY RESOURCES TABLE

Reagent or resource	Source	Identifier
<b>Experimental models: Organisms/strains</b>		
Non-human primate ( <i>Macaca mulatta</i> )	California National Primate Research Center	N/A
<b>Software and algorithms</b>		
MATLAB	The Mathworks	<a href="https://www.mathworks.com/products/matlab.html">https://www.mathworks.com/products/matlab.html</a>
The Multichannel Acquisition Processor (MAP) Neurophysiology System	Plexon	<a href="https://plexon.com/">https://plexon.com/</a>
Offline Sorter	Plexon	<a href="https://plexon.com/">https://plexon.com/</a>
MonkeyLogic Toolbox for MATLAB	NIH	<a href="https://www.brown.edu/Research/monkeylogic/">https://www.brown.edu/Research/monkeylogic/</a>
Custom analysis code	This paper	<a href="https://zenodo.org/record/5708963">https://zenodo.org/record/5708963</a>
ISCAN	ISCAN	<a href="http://iscaninc.com/home.html">http://iscaninc.com/home.html</a>
Adobe Illustrator	Adobe Inc.	<a href="https://www.adobe.com/">https://www.adobe.com/</a>

## RESOURCE AVAILABILITY

## Lead contact

Further information and requests for resources and reagents should be directed to and will be fulfilled by the lead contact, Erin L. Rich ([erin.rich@mssm.edu](mailto:erin.rich@mssm.edu)).

## Materials availability

This study did not generate any new unique reagents.

## Data and code availability

All data reported in this paper will be available by the lead contact upon request.

All original code has been deposited at Zenodo and is publicly available as of the date of publication. DOI are listed in the [key resources table](#).

Any additional information required to reanalyze the data reported in this paper is available from the lead contact upon request.

## EXPERIMENTAL MODEL AND SUBJECT DETAILS

All procedures were in accord with the National Institute of Health guidelines and the recommendations of the University of California, Berkeley Animal Care and Use Committee. Subjects were two male rhesus monkeys (*Macaca mulatta*), Q and R, aged 5 and 6 years, and weighing approximately 7 and 9 kg at the time of recording. Monkeys worked for diluted fruit juice rewards and daily fluid intake was regulated to maintain motivation. Subjects sat head-fixed in a primate chair and viewed a computer screen. MonkeyLogic software (Asaad and Eskandar, 2008) controlled the behavior interface and subjects' eye movements were tracked with an infrared camera (ISCAN). Subjects each had two circular recording chambers (Crist instrument, Inc.) situated over the bilateral prefrontal cortex.

## METHOD DETAILS

## Spatial self-ordered search task

We analyzed data from two monkeys performing a spatial self-ordered search task with six identical visual targets. Behavior and single unit data were previously reported in (Chiang and Wallis, 2018b). On each trial, subjects were presented with a configuration of six targets and were required to saccade to each target, one at a time in any order, returning their eyes to the center after each target (Figures 1A and 1B). Reward was only delivered the first time each target was selected within a trial. Any revisited target resulted in a 500ms time-out with a red square presented on the full screen. Therefore, subjects had to use WM to track and update which targets had already been selected and prepare for the next target selection. A trial was completed when all six targets

had been selected. To avoid frustration, the trial was terminated as incomplete if there were 10 consecutive time-outs within a trial. On average, numbers of completed trials per block were  $38.4 \pm 0.2$  and  $34.8 \pm 0.7$  for subject R and Q, respectively. For each new trial, the target-reward contingency was reset after the inter-trial interval (2 s). The target color was the same within a trial, but changed in a sequence of green-blue-white at the onset of a new trial to ensure that subjects realized reward contingencies were reset. Target configurations remained the same for blocks of 40 trials ( $\geq 240$  selections), enabling us to quantify selection patterns. The spatial configuration of targets used for each block was pseudorandomly chosen from a pool of 20 *a priori* designed spatial configurations. We ensured that targets were distributed relatively evenly across the display so that the centroid of each target configuration was located within  $\pm 3^\circ$  of the window around the fixation cue. The same configuration was presented repeatedly within a block but used in only one block per session. Subjects were able to complete 6 blocks per session (240 trials, or  $\geq 1440$  selections). Only one block of data with less than 20 complete trials in subject Q was removed from analysis. In total, we analyzed 90 blocks in 15 recording sessions from subject R and 59 blocks in 10 recording sessions from subject Q (Table S1). Only completed trials were included in the analyses.

We calculated SI as previously described (Chiang and Wallis, 2018b) to quantify the subject's target selection patterns. For each block of trials, we counted how often each target (target A to F) was selected first, second, etc. and created a matrix of selection frequencies (e.g., Figure 2A), with dimensions of six selections by six targets. These matrices were sorted according to the most common sequence in which the targets were selected. SI quantified the extent to which the subject searched through the targets in the same sequence for all completed trials within a block and was defined as:

$$SI = (a - b) / (a + b) \quad (\text{Equation 1})$$

where  $a$  is the sum of the entries on the main diagonal of the matrix and  $b$  is the off-diagonal sum of the matrix. Our previous results had shown that higher SIs significantly improved behavioral performance, evident as a reduction in the number of revisited targets for both subjects (Chiang and Wallis, 2018b).

We compared behavior between high and low SI blocks, defined by a median split of observed SIs within session for each monkey. Common selection patterns were followed more frequently on high SI compared to low SI blocks (Two-way ANOVAs: H/LSI blocks,  $p < 0.001$  for both subjects), and the pattern is clearly present throughout all 6 selections, indicating that high SI's aren't exclusively driven by first or last target effects (Figure S2D). RTs were calculated as the time from configuration presentation to target selection. A multiple linear regression model predicted RTs from saccade order, high/low SI block, and the order  $\times$  block interaction. Errors with respect to sequence position were previously analyzed by determining the difference between observed and expected success rates (Chiang and Wallis, 2018b). Expected success rates were calculated by assuming that errors are a linear function of the number of potentially incorrect saccades that are possible. That is, it's impossible to make a mistake on the first target selection, and highly unlikely on the second (1/6, or 16.7% chance), etc., so that success rates should show a linear decline with each target selected if errors are randomly distributed. The other possibility is that monkeys use WM and memory strategies, so that they perform better than the expected success rates when WM loads are low, but performance suffers when WM capacity is exceeded. Therefore, the expected success rates were calculated by fitting a linear function to the average success rate across all target selections, such that there is a consistent decrease at each target selection. This calculation assumes that there is a baseline error rate and the only factor distributing these errors is task statistics that change the probability of selecting a correct target by chance.

### Neurophysiological procedures

Our methods for neurophysiological recording have been reported in detail previously (Chiang and Wallis, 2018b). In brief, both subjects were implanted with a titanium head positioner and recording chambers over each hemisphere. Chamber position was determined from previously acquired 1.5-T MRI scans to target the dorsal and ventral banks of the principal sulcus. Neurons were recorded from bilateral LPFC with 12–16 tungsten microelectrodes (FHC Instruments), advanced with custom built, manual microdrives in each recording session. Electrodes were placed in the target area by mapping the position of sulci and gray and white matter boundaries during recordings. Within the target area, we randomly sampled neurons and did not attempt to filter neurons based on selectivity. In total, 1077 units were collected from both monkeys (Subject R: 709; subject Q: 368), the majority of which were within the principal sulcus. The number of recording units per session are listed in Table S1. Waveforms were digitized (Plexon Inc.) and stored for offline spike sorting (Offline Sorter, Plexon Inc.) and analysis.

### QUANTIFICATION AND STATISTICAL ANALYSIS

We conducted all statistical analyses using custom MATLAB (Mathworks) scripts. Data included in the analyses were from six correct saccades in completed trials. For each neuron, we calculated its mean firing rate (FR) during the hold target epoch, which comprised the 500ms period of fixation required to select a target, or during the sliding epochs of 200ms windows stepped forward by 10ms. The size of the neural ensembles corresponded to the number of neurons recorded per session (Table S1). In decoding analyses, we treat each simultaneously recorded ensemble as independent and do not pool neurons into a pseudo-population.



### Spatial tuning

Responses of single neurons are described in detail in [Chiang and Wallis \(2018b\)](#). Briefly, the firing rate of each neuron was computed in a 500 ms window during the hold-target epoch, and fit with a linear model that included the following predictors: X and Y coordinates of the selected target, saccade order position, target distance from fixation, SI in the block, X and Y coordinates of the previous target selected, X and Y coordinates of the next target selected, and target color ([Table S2](#)). To quantify changes in spatial tuning across the population, we used the same analysis windows and converted target locations to polar coordinates to compute the magnitude and direction of the resultant vectors for standardized firing rates in response to each target selection. Changes in spatial tuning were quantified by splitting each session into high and low SI blocks (median split), and calculating one resultant vector for each block type, then finding the change in direction ( $d^\circ$ ) and magnitude ( $m^\circ$ ) of these vectors ([Figure 2](#)).

### Categorical decoders

We used LDA with leave-one-out cross validation to decode task features, as implemented by the MATLAB function *classify*. A diagram in [Figure S1](#) illustrates the decoders we used to classify target locations, saccade orders, and target colors, separately. The feature matrix consisted of average firing rates in a given epoch observed during each correct saccade (rows) from each neuron (columns), and labels were target identity, as determined by its spatial location (e.g., target A, B, etc.), saccade number (e.g., saccade#1, #2, etc.), or target color (green, blue, and white). Classifiers were separately trained and tested on each block of 40 trials ( $\leq 240$  correct saccades). Performance was quantified as either the percent of saccades accurately classified when held out from the training set, or the decoding accuracy of the correct category for the held-out observation ([Figure S2](#)). Mean decoding performance was calculated as the mean number of held-out trials classified correctly from all saccades. To examine whether decoding was affected by SI, we performed two-way ANCOVAs on mean decoding performance with continuous variable SI and two categorical variables: target location and saccade order. Significance was evaluated at  $p < 0.05$  unless otherwise specified.

### Two-dimensional spatial decoder

The LDA tested whether neural activity distinguished different targets categorically, but cannot determine whether these codes are based on spatial coding or other distinctions. To examine how well target locations could be predicted, we used a regularized general linear model with 10-fold cross validation as a continuous variable decoder to predict the locations of selected targets ([Astrand et al., 2016](#)). A diagram in [Figure S1](#) illustrates the data structure. The feature matrices were the same as those of categorical decoders, and labels were either X- or Y-coordinates corresponding to each selected target. Regularization was implemented with the MATLAB function *ridge*. Ridge regression is a regularization method to prevent overfitting ([James et al., 2013](#)). In order to find the optimal ridge parameter,  $k$ , we calculated the mean square error (MSE) between predicted and actual values ([Figure S5](#)). We used a 2-step grid search procedure for optimization. First, we searched a wide parameter space that was coarsely sampled ( $k = 10^1$ ,  $t = -8:1:8$ ), to find the parameter that most frequently minimized MSE in 100 iterations, each using 10-fold cross validation. We used these results to narrow the search space and sample more precisely. We repeated the above procedure with 100 evenly spaced parameters  $t'$ , where  $k = 10^1$ , and  $10^{t-2} \leq t' \leq 10^{t+2}$ . Optimal  $k$  was again based on the minimum MSE. Accuracies were quantified as the Euclidean distance between actual and predicted targets in 2-D space ([Figure S5](#)).

### Noise correlations

Noise correlations are defined as shared variability among neurons that can be detected across repeated presentations of identical stimuli ([Cohen and Kohn, 2011](#)). Our task design is somewhat unconventional for calculating noise correlations, since there is variability in both saccade order and target location so there are few repeated presentations of stimuli that could be considered both perceptually and cognitively identical. Therefore, we approximated noise correlation measures separately for each selected target location or sequence position, as if it were repeated measures of an identical stimulus. To calculate correlated activity at each sequential position, we performed pairwise Pearson correlations separately on all first saccades, second saccades, etc. across all trials within each block. These analyses removed signal correlations due to saccade order, since each saccade was examined separately, and shuffled signal correlations due to target location, since the data were sorted with respect to saccade number, not target. Likewise, to calculate correlated activity across saccades to the same target location, we performed pairwise Pearson correlations separately on all selections of target A, B, etc., across all trials within each block. These analyses removed signal correlations due to target location, since each selection was examined separately, and shuffled signal correlations due to saccade order, since the data were sorted with respect to target, not saccade number. Further, we minimized the risk of falsely inflating the correlation values by excluding correlations between units on the same electrode from analysis ([Leavitt et al., 2013](#)). After applying this exclusion criterion for each recording session, on average we had  $1118.1 \pm 131.1$  and  $658.2 \pm 71.1$  pairs of noise correlation from  $47.3 \pm 2.7$  and  $36.8 \pm 2.1$  simultaneously recorded neurons on subject R and Q, respectively. Fisher's r-to-z transformation was applied to the correlation coefficients in order to normalize variance for hypothesis testing. As previously reported ([Leavitt et al., 2013](#); [Tremblay et al., 2015](#)), we found different pairs of neurons had positively and negatively correlated activity. We reasoned that positive and negative noise correlations may be differentially related to sequencing strategies, so we separately calculated the proportion of neurons with significant positive or negative noise correlations as a function of SI in each block (Pearson correlations). This was carried out in four different epochs: early and late fixation (500ms non-overlapping bins from the 1 s fixation window), the hold target epoch, and the reward delivery epoch ([Table S4](#)).

### Neuron dropping procedure

To determine the contribution of each neuron to ensemble decoding, we reran the LDA analyses with a neuron dropping procedure (Narayanan et al., 2005). We removed one neuron at a time from the whole neural ensemble ( $n$ ), ran the classifier with the remaining ensemble ( $n-1$ ), and found the change in decoding performance between ensembles  $n$  and  $n-1$ . Performance was quantified by calculating the decoding accuracy between actual and predicted classes across saccades in a given block. Thus, removing an informative neuron will decrease decoding performance, but removing a noisy or redundant neuron will have little effect or even increase performance. A median baseline performance was also calculated from all  $n-1$  ensembles in a block (Figure 5A), and used to define high and low contribution subgroups of neurons as those that produced performance drops below or above the median respectively. To further quantify each neuron's contribution, we created a standardized contribution index for each unit in each block.

$$\text{Contribution index} = [\text{Prob}(n) - \text{Prob}(n-i)] / \text{Prob}(n) \quad (\text{Equation 2})$$

The contribution index of the  $i$ -th neuron is defined as the ratio of the difference between the mean decoding accuracy from the full ensemble ( $n$ ) and the remaining ensemble ( $n-i$ ) after removing neuron  $i$ . In Equation 2,  $\text{Prob}(n)$  denotes the mean decoding performance from the full ensemble,  $\text{Prob}(n-i)$  denotes the same mean decoding performance from the  $n-i$  ensemble. If the contribution index was positive, the  $n-i$  ensemble had lower decoding accuracy compared to the full ensemble, and the  $i$ -th single neuron improved decoding. More positive CIs indicated a bigger drop in performance, so that the neuron made a larger contribution to the ensemble. On the other hand, if the CI was negative, then neuron  $i$  reduced decoding, and if it equaled 0, there was no difference between the full and reduced ensemble. In the latter case, the  $i$ -th unit either provided redundant information or made no contribution. CIs were calculated separately for each block, resulting in 4254 data points for subject R and 2171 data points for subject Q. We then excluded data points with zero contribution indices [573 out of 4254 for subject R; 289 out of 2171 for subject Q] for the further analysis.

### Optimal ensemble size measures

To assess the optimal ensemble size for each decoder in trial blocks, we adopted BSU and BE procedures from previous work (Backen et al., 2018). First, we decoded each feature (target identity, saccade number, target color) from each single unit within a block, and sorted the neurons according to descending accuracy. Then, for the BSU procedure, we iteratively added each neuron to an accumulating ensemble in the sorted order, starting with the most informative, and ran the LDA as previously described to determine accuracy at each step. The BE procedure was similar, starting with the most informative neuron, but considered all possible combinations of neurons with each new addition, keeping the unit that yielded the highest accuracy for that ensemble size. After either BSU or BE, the optimal ensemble size was defined by how many neurons were included in the neural ensemble to reach the maximum decoding accuracy (PCT100), or 90%, 75%, or 50% of maximum (PCT90, PCT75, PCT50).

### Dimensionality measurement

Dimensionality can be quantified by different measurements in different tasks and neural systems (Abbott et al., 2011; Ganguli and Sompolinsky, 2012; Gao and Ganguli, 2015; Rigotti et al., 2013). Here, we used the PR, calculated as a continuous measurement of dimensionality by using the population activity patterns from every correct saccade in each trial, to assess variability. The PR is closely related to the concept of explained variance from principal component analysis (Dąbrowska et al., 2021; Gao et al., 2017) and is defined as:

$$\text{PR} = \frac{\left(\sum_{i=1}^M \mu_i\right)^2}{\sum_{i=1}^M \mu_i^2} \quad (\text{Equation 3})$$

Where  $\mu_i$  are the eigenvectors of a covariance matrix for  $i = 1$  to  $M$  simultaneously recorded units. To calculate PR, we first created spike-count arrays from simultaneously recorded units, consisting of 20ms non-overlapping bins in four 500ms epochs (early fixation, late fixation, hold target, and reward epochs), for each correct saccade in a given trial (Figure S1). Then, we calculated the covariance (COV) for each array, which indicated how the population covaries across epochs (Gao et al., 2017), and calculated the vector  $\mu$  containing the eigenvalues of the square matrix COV. The size of the square matrix COV is equal to  $M$  simultaneously recorded units. Lastly, we created a vector of PR values for each correct saccade in blocks of complete trials to assess changes in dimensionality across saccades. In general, the PR corresponds to the number of dimensions required to explain about 80%–90% of the total population variance (Gao et al., 2017). In other words, the diversity of firing patterns in the neural ensembles increased with PR. To compare PR values across recording sessions, we normalized vectors of PR within a session before further analyses. The linear model was calculated for each monkey as follows:

$$\text{PR} \sim b1.\text{Saccades} + b2.SI + b3.nSigs \quad (\text{Equation 4})$$

where *Saccades* is the saccade number within a trial, *SI* is calculated from behavior in each block, and *nSigs* is the number of neurons in each ensemble (Table S1).